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Designing a universal income support mechanism for Italy. An exploratory tour

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# Designing a universal income support mechanism for Italy. An exploratory tour 

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#### Abstract

Differently from most European countries and despite the recommendations on the part of the European Commission, Italy still misses a sufficiently systematic and nationwide mechanism of income support. In this paper we explore the feasibility, the desirability and the features of a universal policy of minimum income in Italy. We use a microeconometric model and a social welfare methodology in order to evaluate various alternatives mechanisms. We simulate the effects and the social welfare performance of 30 reforms resulting from six versions of five basic types of income support mechanism: guaranteed minimum income (GMI), universal basic income (UBI), wage subsidy (WS) and two mixed systems: GMI+WS and UBI+WS. As welfare evaluation criteria we adopt the Gini Social Welfare function and the Poverty-Adjusted Gini Social Welfare function. All the reforms are calibrated so as to preserve fiscal neutrality. The simulation adopts a methodology that allows for market equilibrium and ensures a consistent comparative statics interpretation of the results. Universal and non mean-tested transfers (possibly complemented by wage subsidy) emerge as desirable and feasible features of the income support mechanism. In the most realistic scenarios, the social-welfare-optimal policies are an unconditional transfer combined with a wage subsidy (a total benefit amounting to about $70 \%$ of the poverty level) or - depending on the social welfare criterion - a more generous pure unconditional transfer amounting to $100 \%$ of the poverty level. In this exercise the reforms can be financed by proportionally increasing the current marginal tax rates and widening the tax base to include all personal incomes, with top marginal rates close to ones currently applied in the Scandinavian countries. The set of universalistic policies that are preferable to the current system is anyway very large and appears to give the opportunity of selecting a best reform according to many different criteria or constraints.


Keywords: Income Support Mechanisms, Basic Income, Guaranteed Minimum Income, Wage Subsidies, Tax Reform Simulation.
JEL Classification: H31, H21, C25.

[^0]
## 1. Introduction

Differently from most European countries and despite the recommendations on the part of the EC, Italy still misses a sufficiently systematic and nationwide mechanism of income support, although various selective or conditional income maintenance policies are operating and some local authorities are experimenting forms of minimum income policy. ${ }^{1}$ In this paper we explore the feasibility, the desirability and the features of a universal policy of income support in Italy. The starting point is provided by optimal taxation theory, i.e. we aim at designing an income support mechanism that replaces the actual policies and maximizes a given social welfare function subject to a public budget constraint. However, instead of looking for an analytical solution we adopt a computational-empirical approach. Namely, we use a microeconometric model and a social welfare methodology in order we explore and evaluate various alternatives mechanisms. In illustrating the motivations, the methods and the results, we will refer to five issues that emerge as crucial in the analysis of reforms, whether hypothetical or implemented:

1) Is a universal income support mechanism feasible and desirable? Universality promises to bring benefits in terms of transparency, simplicity and lower incentives for wasteful lobbying and rent-seeking. We will investigate whether universalistic reforms are feasible with respect to the public budget constraint and desirable according to a social welfare criterion.
2) Should the mechanism consist of a transfer or a subsidy or a combination of the two? A significant part of the recent literature on the design of income support mechanisms is focussed on comparing transfer-like policies (such as the negative income tax, the demogrant, the basic income etc.) versus subsidy-like policies (such as earned income tax credit, in-work benefits etc.). The former permit the attainment of a minimum level of income through a lump-sum transfer, while the latter provide the opportunity of receiving a higher income by supporting a higher net age rate. Most numerical simulations done with the model of Mirrlees (1971) suggest as an optimal system a tax-transfer schedule with a lump-sum transfer, very high marginal tax rates on low income and almost constant marginal tax rates on average and high income. This scenario seems to have inspired many reforms (implemented or discussed) in the three decades 1970-80-90. A second scenario emerges since the end of the 90 s, with contributions (e.g. Diamond (1998) and Saez (2001, 2002)) that make Mirrlees' model more amenable to econometric applications and generalize it to include the decision of whether to work or not (not only - as in Mirrlees (1971) - the decision of how much to work). This latter extension is particularly relevant for the design of income support mechanisms. An influential contribution is represented by in particular by Saez (2002), whose model has been adopted in various applications (e.g. Immervoll et al., 2007; Haan et al., 2007; Blundell et al.,

[^1]2009). A frequent result emerging from these studies is the superiority of policies such as in-work benefits, or taxcredit on low earnings. Interestingly, analogous policies have been in part implemented or considered as alternatives to mean-tested transfers in various countries during the last decade. The theoretical nature of the optimal taxation literature in practice has forced the analysis to address transfer-based and subsidy-based mechanisms as if they were strictly alternative. But nothing prevents the design of mechanisms that combine the two policies. In what follows we will also consider such mixed policies.
3) Should a transfer be conditional or unconditional (mean-tested)? Besley (1990) concludes for the superiority of mean-testing, on the basis however of a rather simple and restrictive theoretical model. The transfers mentioned at point 2 ) are typically conditional. So far the idea of a universal and unconditional transfer has never reached the position of a dominating scenario but it remains an inspiring idea with oscillating fortunes. ${ }^{2}$ It has strong philosophical motivations (e.g. Van Parjis 1995), but also arguments based on efficiency and incentives are sometimes put forward. Besides avoiding the costs of verifying and monitoring the eligibility conditions, unconditional transfers do not create poverty traps and there is evidence that they can promote more efficient choices in education, production and occupational career (Barrientos and Lloyd-Sherlock 2002, Standing 2008). Atkinson (2002) suggests that various processes in the modern economies might naturally drive the social policy institutions toward the universal basic income scenario. ${ }^{3}$ Given the model and the data used, our study will only be able to throw light on the issues of the relative redistributive performance, the poverty trap and the incentives to participation.
4) How generous should the policy be? Every income support mechanism needs to specify the level of minimum income. This applies to transfer policies since they typically aim at guaranteeing that a certain minimum income is attained. But it also applies to incentive-base policies, since the subsidies are usually active only up to a certain level of income. The typical amount (in proposed or implemented reforms) is not larger than the poverty level and in most cases is much lower. This is so because the mechanisms are designed as complementary with respect to other welfare and social policies. There are however more extreme versions where the amount is supposed to be more substantial either because it is meant to replace the whole welfare state, as in Friedman (1962), or because it is thought as a fundamental political-economic restructuring of the market economy, as in Van Parijs (1995). In this paper we will investigate the performance of transfers or subsidies of different amount up to the Poverty Level.

[^2]5) Should taxes (that also finance the income support mechanism) be progressive or flat? Universal mechanisms of income support (whether transfer-based or subsidy-based) have been frequently presented together with the proposal of a flat-tax. The main motivation was probably to counterbalance the costs and/or the (supposedly) negative incentives coming from income support with better incentive to labour supply for the (supposedly) most productive fraction of the population. However, the above argument ignores the fact that labour supply elasticity is inversely related to income levels (e.g. Aaberge et al. 1999, 2002; Aaberge and Colombino 2011, 2012) and takes it for granted - despite the ambiguous empirical evidence - that income support mechanisms have strong negative effects on labour supply. When taking into account these empirical facts, we might be led instead to support a progressive taxation.

## 2. The alternative policies

In this section we summarize the main features of the hypothetical tax-transfer reforms that will be simulated under the assumption that they completely replace the actual tax-transfer system (a detailed description is provided in Appendix B). They are stylized cases representative of the different scenarios that are discussed or even actually implemented in many countries. A key parameter in the definition of the policies is the threshold G defined as follows. Let $x_{i}=$ total net available income (current) of household $i$ (including both couples and singles).
$N_{i}=$ total number of components of household i.
Define the "individual-equivalent" income: $\tilde{x}_{i}=x_{i} / \sqrt{N_{i}}$ and the Poverty Line $P=\operatorname{median}(\tilde{x}) / 2$. Then $G_{i}=a P \sqrt{N_{i}}$, where $a$ is a proportion. For each reform we simulate three versions with different values of $a: 1,0.75$ and 0.50 . For example, $G=0.5 P \sqrt{3}$ means that for a household with 3 components the threshold is $1 / 2$ of the Poverty Line times the equivalence scale $\sqrt{3}$. ${ }^{4}$

Guaranteed Minimum Income (GMI). Each individual receives a transfer equal to $G-I$ if single or $G / 2-I$ if partner in a couple provided $I<G$ ( or $I<G / 2$ ), where $I$ denotes individual taxable income. This is the standard conditional (or means-tested) income support mechanism, close to a Negative Income Tax (Friedman 1962; Tobin 1966) with a 100\% marginal reduction rate of the transfer.

[^3]Unconditional Basic Income (UBI). Each individual receives an unconditional transfer equal to $G$ if single or $G / 2$ if partner in a couple. It is the basic version of the system discussed for example by Van Parijs (1995) and also known in the policy debate as "citizen income" or "social dividend" (Meade 1995; Van Trier 1995). ${ }^{5}$

Wage Subsidy (WS). Each individual receives a $10 \%$ subsidy on the gross hourly wage and her/his income is not taxed as long as her/his gross income (including the subsidy) does not exceed $G$ if single or $G / 2$ if partner in a couple. This is close to various in-work benefits or tax-credits reforms introduced in the USA (Earned Income Tax Credit), in the UK (In-Work Benefits) and recently also in Sweden.

GMI + WS and UBI + WS are mixed mechanisms where the transfer is coupled with the wage subsidy, but with the threshold redefined as $0.5 G{ }^{6}$

For each of the above five types we distinguish two versions: a flat tax version, in which the income support mechanism is matched with a fixed marginal tax rate $t$ applied to individual incomes above $G$ for singles or $G / 2$ for the partners of couple; a progressive tax version, in which the income support mechanism is matched with a progressive tax (that replicates the current system but with marginal tax rates proportionally adjusted according to a constant $\tau$ ) that applies to incomes exceeding $G$ (or $G / 2$ ). The parameters $t$ and $\tau$ are endogenously determined within the reform simulation so that the total net tax revenue is equal to the one collected under the current tax-transfer system. Altogether we have 5 (types) $\times$ 3 (values of $a) \times 2($ tax rules $)=30$ reforms .

## 3. The microeconometric model

We develop a microeconometric model of household labour supply that is capable of simulating the household choices, taxes paid, transfers received, net available income and attained utility level given any tax-transfer rule regime, under the constraint of a constant total net tax revenue.

Appendix A provides a detailed description of the model. Here we offer an intuitive overview. Although we actually treat both couples and singles, for the sake of simplicity the following illustration considers singles.
The model assumes the households choose a job from alternatives characterized by hours of work $h$; other characteristics of the job-household match are denoted by $j$. The problem solved by the agent is the following:

$$
\begin{aligned}
& \max _{(h, j) \in \Omega} U(C, h, j) \\
& \text { s.t. } \\
& C=R(w h, y)
\end{aligned}
$$

[^4]where
$h=$ hours of work,
$w=$ the pre-tax wage rate,
$j=$ unobserved (by the analyst) characteristics of the household-job match,
$y=$ the pre-tax non-labour income (exogenous),
$C=$ net disposable income,
$R=$ tax rule that transforms gross pre-tax incomes $(w h, y)$ into net disposable income $C$,
$\Omega=$ the set of all opportunities available to the household (including non-market opportunities, or "leisure" activities, i.e. "jobs" with $h=0$ ).
Households can differ not only in their preferences and in their wage (as in the traditional model) but also in the number of available jobs of different types. Let $p(h)$ denote the relative frequency of available jobs of type $h$. By representing the choice set $\Omega$ by a probability density $p$ we can, for example, allow for the fact that jobs with hours of work in a certain range are more or less likely to be found, possibly depending on households' characteristics; or for the fact that for different households the relative number of market opportunities may differ. We assume that the utility function can be factorised as
$$
U(R(w h, y), h, j)=V(R(w h, y), h)+\varepsilon(j)
$$
where $V$ and $\varepsilon(j)$ are respectively the systematic and the random component. The term $\varepsilon(j)$ is a random variable that accounts for the effect on utility of all the characteristics of the household-job match that are observed by the household but not by us. Assuming that $\varepsilon(j)$ is i.i.d. according to the Type I Extreme Value distribution, it can be shown that we can write the probability of a choice $(h)$ as $^{7}$
$$
\varphi(h)=\frac{v(R(w h, y), h) p(h)}{\sum_{H} v(R(w H, I), H) p(H)}
$$

The intuition is that the probability of a choice $h$ can be expressed as the relative attractiveness - weighted by a measure of "availability" $p(h)$ - of jobs of type $h$. Given convenient parametric specifications of the functions $V$ and $p$, the parameters of the model can be estimated by maximizing likelihood. The estimated model can then be used to simulate the effect of a reform by replacing the current tax-transfer function, say $R^{0}$, with the new one, say $R^{1}$.

[^5]
## 4. Social Welfare evaluation

Since the tax-transfer reforms in general have different effects on different households we need a criterion to "aggregate" all the micro-effects into a synthetic index in order to be able to compare and evaluate the reforms. We will use two indexes. The first one is based on $\operatorname{Sen}(1974,1976)$, who proposed to compare different statuses of the economy by computing namely $\mu(1-I)$, where $\mu$ is the average income and $I$ is the Gini coefficient of the income distribution. This measure has the intuitive appeal of expressing social welfare as the product of an efficiency measure (average income, i.e. the average size of the "pie's slices") time a familiar equality measure (1-I), i.e. a measure of how equally the "pie" is allocated among the households). We apply the same idea using money-metric utility instead of income. Let $\mu^{n}(R)$ be the maximum money-metric utility attained under tax-transfer regime $R$ by household $n$ (computed as explained in Section A. 7 of Appendix A) and $\mu(R)=\sum_{n} \mu^{n}(R) / N$. Let $I(R)$ be the Gini coefficient of the sample distribution of $\mu^{n}(R)$. We then define the Gini Social Welfare (GSW) function as follows: ${ }^{8}$
$G S W(R)=\mu(R)(1-I(R))$.
The second index - the Poverty-adjusted Gini Social Welfare (PAGSW) - is a generalization that gives a specific weight to poverty (Atkinson 1987):
$\operatorname{PAGSW}(R)=\mu(R)(1-I(R)-p(R))$
where $p(R)$ is the head-count poverty ratio under the tax-transfer regime $R$.

## 5. Simulation procedure

The simulation has two distinctive features that are not common in the tax reform literature. First, the reforms are simulated under the constraint of being fiscally neutral, i.e. they generate the same total net tax revenue as the current 1998 system. This requires a two-level simulation procedure. At the "low" level, household choices are simulated given the values of the tax-transfer parameters. At the "high" level, the tax-transfer parameters are calibrated so that the total net tax revenue remains constant. The calibration parameters are the constant tax rate $t$ in the Flat tax systems and the proportional change $\tau$ of the current marginal tax rates in the Progressive tax systems. ${ }^{9}$ Second, the simulation is conducted under equilibrium conditions for different hypothetical values of the elasticity of the demand for labour. Traditionally, the simulation of tax reforms are interpreted as comparative statics exercises in a long-run perspective, i.e. assuming a perfectly elastic labour demand (constant wage rates). At the other extreme, non-behavioural simulations can

[^6]be interpreted as simulations in the very short-run. There are of course an infinity of intermediate scenarios. We adopt a procedure that is specifically appropriate for the microeconometric model and makes the simulation results consistent with the comparative statics interpretation. The procedure is fully explained in Colombino (2010) and more concisely in Appendix A.

We perform six types of simulations, corresponding to different treatment of equilibrium:
Non behavioural. Household choices are left unchanged, while their incomes are changed according to the new taxbenefit rules. This can be considered as a prediction of the very short-run.

No account for equilibrium. This is the standard procedure. Labour supply responses are simulated while keeping wage rates unchanged. Usually this is interpreted as a long run prediction under the hypothesis of a perfectly elastic demand for labour. However, as we argue in Appendix A, this interpretation in general is not correct when adopting a model that incorporates a representation of demand condition (the multinomial logit with alternative-specific dummies).

Demand elasticity $\boldsymbol{\eta}=\mathbf{0}, \mathbf{- 0 . 5}, \mathbf{- 1}$. Most empirical studies of wage elasticity of the demand for labour suggest values in the range $(-0.5,-1)$.

Demand elasticity $\boldsymbol{\eta}=-\infty$. This is a theoretical benchmark. It should be interpreted as indicating the direction towards which we move if we assume a very elastic demand.

We consider as realistic scenarios those with $\eta=-0.5$ and $\eta=-1$. The other cases are reported as benchmarks.

## 6. Results

Tables 1-3 illustrate the main welfare evaluation results. More detailed results are reported in Appendix C. We start by commenting the results of Tables 1 and 2 following the five-issue outline introduced in section 1 . Moreover, if not otherwise indicated, we refer to the results obtained under the most realistic scenarios, i.e. $\eta=-0.5$ or -1 . The policies (30 reforms plus the current system) are ranked - the most preferred on top - according to the social welfare functions presented in section 4 . Each reform is identified by three pieces of information: the income support mechanism (GMI etc.), the Flat (F) or Progressive (P) tax rule and the value of $a(0.5,0.75$ or 1$)$. For example, UBI+WS_F_0.75 denotes a policy where the income support mechanism is UBI+WS, the tax rule is Flat and $G=0.75 P \sqrt{N}$.

1) Most reforms rank better than the current system under both social welfare criteria. The only exception appears when $\eta=-\infty$ and the policies are ranked according to GSW: in this case, no reform turns out as preferred to the current system. However $\eta=-\infty$ represents a benchmark case rather than a realistic scenario. In all the other cases there is a very large menu of universalistic reforms that dominate (in terms of welfare) the current system. Therefore the answer to the first issue mentioned in section 1 is definitively affirmative. As we comment below, the welfare criteria adopted here gives specific answers as to what mechanisms are best. However, also from the
point of view of different criteria, we have many alternatives among which to choose in order to improve upon the current system.
2) In most cases, the first four or five positions in the ranking are occupied by transfer-based mechanisms or by mixed policies envisaging both transfers and subsidies. Under this respect, we observe a marked difference between the GSW criterion and the PAGSW criterion. The former criterion favours the mixed policy UBI+WS while the latter favours a pure UBI.
3) Overall, mechanisms envisaging unconditional transfers (UBI or UBI+WS) rank better than the conditional systems. The greater generosity of the unconditional transfers is compensated by the lack of poverty-trap effects, so that both the conditional and the unconditional systems imply similar very modest reductions in labour supply; however, the unconditional systems perform better in favouring distributional equity and reducing poverty. ${ }^{10}$
4) Under GSW, the benefit (transfer + subsidy) should be $75 \%$ of the poverty line; under the PAGSW it should be $100 \%$.
5) In most cases Progressive tax systems are preferable to Flat tax systems. A contribution to this result comes from the pattern of wage elasticity of labour supply: higher income households are much less elastic than lower income ones (Aaberge et al. 1999, 2002, 2004; Aaberge and Colombino 2011, 2012; Røed and Strøm 2002). ${ }^{11}$

In summary, the indications for a best mechanism converge on UBI+WS_P_0.75 (under the GSW criterion) or UBI_P_1 (under the PAGSW criterion).

In Table 3 we report the result of a regression analysis of the results obtained under the scenario with $\eta=-1$. The value of the Social Welfare function is regressed against a set of variables measuring the key features of the tax-transfer systems. The regressions help to identify the welfare contribution of policy attributes. Under the GSW criterion, the results confirm that the progressivity of the tax rule and the non-conditionality of the income support mechanism have a significant positive effect. The coverage $a$ has a positive marginal effect up to around 0.70 . The picture produced by the PAGSW criterion is partially different. Overall the coefficients are much larger, since there is much more variation in the GSW than in the PAGSW. The effects of Progressive and Unconditional are positive as under the GSW, but less significant. Instead the effect of Subsidy is negative and significant. Coverage has a positive marginal effect even above 1.

What specific features do the best mechanisms have and how do they fare from the perspective of other possibly relevant criteria, such as marginal tax rates or behavioural effects? Tables C. 1 - C. 6 of Appendix C provide many relevant details. Here the policies are listed in alphabetic order. For each type of simulation (No Behaviour, No Equilibrium etc.) and for

[^7]each policy the tables report the results listed in the Legenda preceding the tables The following comments consider what happens under the scenario with $\eta=-1$ (Table C.5).

1) UBI+WS_P_0.75 (UBI_P_1) envisages an average monthly benefit (transfer + subsidy) per household of 720 (1060) Euros 1998, which represent about $70 \%$ ( $100 \%$ ) of the Poverty Level. This amount is to be compared with the 101 Euros of the CURRENT system. ${ }^{12}$ The percentages of utility-winners and of income-winners are respectively 69 (57) and 65 (58). The percentage poverty rate (head count) is 0.9 (0), to be compared to 4.23 under the CURRENT system.
2) Typical objections against universalistic policy of income support are based on the expectation of high tax rates required by the public budget constraint and of strong disincentive effects on labour supply. The first expectation is confirmed by our results. The best (welfare-wise) policies are costly in terms of marginal tax rates.

UBI+WS_P_0.75 would require an $11 \%$ increase of the current (1998) marginal tax rates, which means a $50 \%$ top marginal tax rate. Under the same scenario UBI_P_1 requires a $60 \%$ top marginal tax rate. It should be noticed that these figures are high but not at all unrealistic. For example in 2009 the top marginal tax rates in Denmark and Sweden were respectively around $62 \%$ and $57 \%$. If the above tax rates were judged for some reasons not feasible (possibly from the point of view of political consensus), however we have already noticed that the тепи of welfare improving reforms is very large. For example, the flat version UBI+WS_F_0.75 would require a $42 \%$ flat rate. Moreover, instead of increasing the marginal tax rates on income one might think of a different structure of taxation e.g. increasing taxes on wealth and on (selected) consumption expenditures. The second expectation (strong disincentive effects on labour supply) is not supported by our results: the overall disincentive effects are small.
3) When we account for behavioural responses and for market equilibrium, the policies turn out to be less costly (tax-wise) than when we assume no behavioural responses or we do not account for market equilibrium. In shaping the simulation results there is a subtle interplay between the behavioural responses and the market equilibrium process. Overall, the reform induce a (modest) shift to the left of the labour supply curve, therefore the new market equilibrium requires a higher gross wage rate (provided $\eta>-\infty$ ). The pure effect on taxation of the behavioural responses can be identified by comparing Table C. 1 to Table C. 6 of Appendix C where $\eta=-\infty$ and therefore wage rates remain unchanged. The reform UBI+WS_P_0.75 would require a $14 \%$ increase in current marginal tax rates when assuming no behavioural responses (Table C.1). The same reform would instead require a $12 \%$ increase in current marginal tax rates when accounting for behaviour (but leaving wage rates unchanged). Despite the overall reduction in labour supply, the reform induces a more efficient composition of employment

[^8]Last, if we assume $\eta=-1$ (Table C.5), the increase would be $11 \%$ : higher gross wage help in collecting tax revenue and therefore the reform requires a lower increase in marginal tax rates.
4) Accounting for behavioural responses and market equilibrium does also have significant implications for the ranking position of the policies. The differences in ranking are more marked when the GSW criterion is used. It seems that with the PAGSW criterion the rankings are strongly influenced by the effects on the head-count poverty index, which in turn are similar across different simulation procedure: as a consequence the differences in rankings are mitigated, especially among the highest rank positions.

## 7. Conclusions

We used a EUROMOD 1998 dataset containing Italian couples and singles aged 20 - 55, a microeconometric model of labour supply and a social evaluation methodology in order to identify feasible and welfare-improving universalistic income support mechanisms in Italy. We consider five type of mechanism: GMI, UBI, WS, GMI+WS and UBI+WS. Each one has three variants, depending on the degree of coverage with respect to the poverty line: $50 \%, 75 \%$ and $100 \%$. Moreover, each type can be match either with Flat tax rule or with a Progressive Tax rule. In total we have $5 \times 3 \times 2=30$ possible reforms. The tax parameter (either constant flat rate in the Flat rule or the proportional change in the marginal tax rates with respect to the current (1998) system in the Progressive rule) is determined endogenously so that the total net tax revenue remains as under the current system. The simulation adopts a methodology that allows for market equilibrium and ensures a consistent comparative statics interpretation of the simulation results (Colombino 2010). Accounting for behavioural responses and market equilibrium has important implications in shaping the simulation results. In the most realistic scenarios (i.e. wage elasticity of labour demand in the range $[-0.5,-1.0]$ ), under the pure Gini Social Welfare (GSW) criterion, the best policy is an unconditional basic income complemented by a wage subsidy (amounting to a benefit close to $70 \%$ of the Poverty Level), while under the Poverty-Adjusted GSW criterion the best policy is a pure unconditional transfer approximately equal to the Poverty Level. More generally, universality, non-conditionality, progressivity, and wage subsidies as a complement to lump-sum transfers (under the GSW criterion) emerge as desirable attributes of an optimal income support mechanism. Evaluation criteria different from the ones chosen in this exercise might of course dictate a different ranking of the policies and different features of the best ones; however the set of policies that are preferable to the current system is very large and suggests the possibility of selecting a universalistic best reform according to many different criteria and constraints.

Table 1. Policies ranked (from best to worst) according to the GSW criterion

| No behaviour |  |  | No equilibrium |  |  | Equilibrium $\boldsymbol{\eta}=0$ |  |  | Equilibrium $\boldsymbol{\eta}=\mathbf{- 0 . 5}$ |  |  | Equilibrium $\boldsymbol{\eta}=\mathbf{- 1}$ |  |  | Equilibrium $\boldsymbol{\eta}=-\infty$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| UBI+WS | P | 1 | UBI+WS | P | 1 | GMI | F | 1 | UBI+WS | P | 0.75 | UBI+WS | P | 0.75 |  | NT |  |
| UBI+WS | P | 0.75 | UBI | P | 0.75 | GMI | F | 0.75 | UBI | P | 0.5 | UBI | P | 0.5 | UBI+WS | P | 0.5 |
| UBI | P | 0.75 | UBI+WS | P | 0.75 | UBI | F | 0.75 | WS | P | 0.75 | UBI | P | 0.75 | GMI+WS | P | 0.5 |
| UBI | P | 0.5 | UBI | P | 0.5 | GMI | P | 1 | UBI+WS | P | 0.5 | WS | P | 0.75 | UBI | F | 0.5 |
| WS | P | 1 | UBI | P | 1 | UBI | F | 0.5 | UBI | P | 0.75 | UBI+WS | P | 0.5 | UBI | P | 0.5 |
| UBI | P | 1 | WS | P | 1 | GMI | P | 0.75 | WS | P | 0.5 | WS | P | 0.5 | WS | P | 0.5 |
| UBI+WS | P | 0.5 | UBI+WS | P | 0.5 | UBI | P | 0.5 | UBI | P | 1 | UBI | P | 1 | WS | F | 0.5 |
| WS | P | 0.75 | WS | P | 0.75 | UBI+WS | F | 1 | GMI+WS | P | 0.5 | GMI+WS | P | 0.5 | GMI+WS | F | 0.5 |
| WS | P | 0.5 | WS | P | 0.5 | UBI | F | 1 | GMI+WS | P | 0.75 | GMI+WS | P | 0.75 | UBI+WS | F | 0.5 |
| UBI | F | 1 | UBI | F | 1 | GMI | P | 0.5 | WS | F | 1 | WS | P | 1 | GMI | P | 0.5 |
| UBI | F | 0.75 | UBI | F | 0.75 | GMI | F | 0.5 | WS | P | 1 | WS | F | 1 | GMI | F | 0.5 |
| GMI+WS | P | 1 | GMI+WS | P | 1 | UBI+WS | F | 0.75 | UBI | F | 1 | UBI | F | 0.75 | UBI+WS | P | 0.75 |
| GMI+WS | P | 0.75 | GMI+WS | P | 0.75 | GMI+WS | F | 1 | UBI | F | 0.75 | UBI | F | 1 | GMI+WS | P | 0.75 |
| GMI+WS | P | 0.5 | GMI+WS | P | 0.5 | UBI | P | 0.75 | UBI+WS | F | 1 | UBI+WS | F | 1 | WS | F | 0.75 |
| WS | F | 1 | UBI+WS | F | 1 | GMI+WS | F | 0.75 | UBI | F | 0.5 | UBI | F | 0.5 | GMI+WS | F | 0.75 |
| UBI+WS | F | 1 | UBI | F | 0.5 | UBI+WS | P | 0.5 | WS | F | 0.75 | GMI | P | 0.5 | WS | P | 0.75 |
| UBI | F | 0.5 | UBI+WS | F | 0.75 | UBI+WS | P | 0.75 | GMI | P | 0.5 | WS | F | 0.75 | UBI | F | 0.75 |
| UBI+WS | F | 0.75 | GMI+WS | F | 1 | UBI+WS | F | 0.5 | UBI+WS | F | 0.75 | UBI+WS | F | 0.75 | UBI | P | 0.75 |
| WS | F | 0.75 | GMI | P | 0.5 | GMI+WS | P | 1 | GMI+WS | F | 1 | GMI+WS | F | 1 | UBI+WS | F | 0.75 |
| GMI | P | 0.5 | GMI | P | 1 | GMI+WS | P | 0.75 | WS | F | 0.5 | GMI+WS | F | 0.75 | GMI | P | 0.75 |
| GMI+WS | F | 1 | GMI | P | 0.75 | GMI+WS | P | 0.5 | GMI | P | 0.75 | WS | F | 0.5 | GMI | F | 0.75 |
| GMI | P | 0.75 | CURRENT |  |  | GMI+WS | F | 0.5 | UBI+WS | F | 0.5 | GMI | P | 0.75 | WS | F | 1 |
| GMI | P | 1 | UBI+WS | F | 0.5 | UBI+WS | P | 1 | GMI+WS | F | 0.75 | UBI+WS | F | 0.5 | GMI+WS | F | 1 |
| CURRENT |  |  | GMI+WS | F | 0.75 | WS | F | 1 | GMI+WS | P | 1 | UBI+WS | P | 1 | WS | P | 1 |
| UBI+WS | $F$ | 0.5 | GMI | F | 1 | WS | P | 1 | UBI+WS | P | 1 | GMI+WS | P | 1 | UBI+WS | P | 1 |
| GMI+WS | $F$ | 0.75 | GMI+WS | F | 0.5 | WS | P | 0.5 | GMI+WS | F | 0.5 | GMI+WS | F | 0.5 | GMI+WS | P | 1 |
| WS | $F$ | 0.5 | GMI | F | 0.75 | WS | F | 0.75 | CURRENT |  |  | GMI | F | 0.75 | UBI | F | 1 |
| GMI+WS | $F$ | 0.5 | GMI | F | 0.5 | WS | F | 0.5 | GMI | F | 1 | CURRENT |  |  | UBI+WS | F | 1 |
| GMI | $F$ | 1 | WS | F | 1 | WS | P | 0.75 | GMI | F | 0.5 | GMI | F | 1 | UBI | P | 1 |
| GMI | $F$ | 0.75 | WS | F | 0.75 | CURRENT |  |  | GMI | F | 0.75 | GMI | F | 0.5 | GMI | P | 1 |
| GMI | $F$ | 0.5 | WS | F | 0.5 | UBI | P | 1 | GMI | P | 1 | GMI | P | 1 | GMI | F | 1 |

Table 2. Policies ranked (from best to worst) according to the PAGSW criterion

| No behaviour |  |  | No equilibrium |  |  | Equilibrium $\boldsymbol{\eta}=0$ |  |  | Equilibrium $\boldsymbol{\eta}=\mathbf{- 0 . 5}$ |  |  | Equilibrium $\boldsymbol{\eta}=\mathbf{- 1}$ |  |  | Equilibrium $\boldsymbol{\eta}=-\infty$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| UBI | P | 1 | UBI+WS | P | 1 | UBI | F | 1 | UBI | P | 1 | UBI | P | 1 | UBI | P | 0.75 |
| UBI | F | 1 | UBI | P | 0.75 | UBI | P | 0.75 | UBI | F | 1 | UBI | F | 1 | UBI | F | 0.75 |
| UBI | P | 0.75 | UBI | P | 1 | UBI | F | 0.75 | UBI | P | 0.75 | UBI | P | 0.75 | UBI | F | 1 |
| GMI | P | 1 | UBI | P | 0.5 | UBI | P | 1 | GMI | F | 1 | GMI | F | 1 | UBI | P | 1 |
| GMI | F | 1 | UBI+WS | P | 0.75 | GMI | P | 1 | GMI | P | 1 | GMI | P | 1 | GMI | P | 1 |
| UBI | F | 0.75 | UBI | F | 1 | UBI+WS | P | 1 | UBI | F | 0.75 | UBI | F | 0.75 | GMI | F | 1 |
| UBI+WS | P | 1 | UBI | F | 0.75 | GMI | F | 1 | UBI+WS | P | 1 | UBI+WS | P | 1 | UBI | P | 0.5 |
| UBI | P | 0.5 | UBI+WS | P | 0.5 | UBI | P | 0.5 | UBI | P | 0.5 | UBI | P | 0.5 | UBI+WS | P | 1 |
| UBI+WS | F | 1 | UBI+WS | F | 1 | UBI+WS | F | 1 | GMI | P | 0.75 | UBI+WS | F | 1 | GMI | P | 0.75 |
| GMI | P | 0.75 | GMI | P | 1 | UBI+WS | P | 0.75 | UBI+WS | F | 1 | GMI+WS | P | 1 | UBI | F | 0.5 |
| UBI | F | 0.5 | UBI | F | 0.5 | GMI+WS | P | 1 | GMI+WS | P | 1 | GMI | P | 0.75 | GMI | F | 0.75 |
| GMI | F | 0.75 | WS | P | 1 | UBI | F | 0.5 | UBI | F | 0.5 | UBI+WS | P | 0.75 | UBI+WS | P | 0.75 |
| UBI+WS | P | 0.75 | WS | P | 0.75 | GMI | P | 0.75 | UBI+WS | P | 0.75 | UBI | F | 0.5 | UBI+WS | F | 1 |
| GMI+WS | P | 1 | WS | P | 0.5 | GMI | F | 0.75 | GMI | F | 0.75 | GMI | F | 0.75 | GMI+WS | P | 1 |
| GMI+WS | F | 1 | UBI+WS | F | 0.75 | GMI+WS | F | 1 | GMI+WS | F | 1 | GMI+WS | F | 1 | GMI+WS | F | 1 |
| UBI+WS | F | 0.75 | GMI | P | 0.75 | UBI+WS | F | 0.75 | UBI+WS | F | 0.75 | UBI+WS | F | 0.75 | UBI+WS | F | 0.75 |
| GMI | P | 0.5 | GMI+WS | F | 1 | GMI+WS | P | 0.75 | GMI+WS | P | 0.75 | GMI+WS | P | 0.75 | GMI+WS | P | 0.75 |
| GMI+WS | P | 0.75 | GMI | F | 1 | UBI+WS | P | 0.5 | GMI | P | 0.5 | GMI | P | 0.5 | GMI | P | 0.5 |
| UBI+WS | P | 0.5 | GMI+WS | P | 0.5 | GMI | P | 0.5 | UBI+WS | P | 0.5 | UBI+WS | P | 0.5 | UBI+WS | P | 0.5 |
| GMI+WS | F | 0.75 | GMI | P | 0.5 | GMI+WS | F | 0.75 | GMI+WS | F | 0.75 | GMI+WS | F | 0.75 | GMI+WS | F | 0.75 |
| GMI | F | 0.5 | GMI+WS | P | 0.75 | WS | P | 1 | WS | P | 1 | WS | P | 1 | GMI | F | 0.5 |
| GMI+WS | P | 0.5 | CURRENT |  |  | GMI+WS | P | 0.5 | GMI | F | 0.5 | GMI | F | 0.5 | UBI+WS | F | 0.5 |
| UBI+WS | F | 0.5 | GMI+WS | P | 1 | UBI+WS | F | 0.5 | UBI+WS | F | 0.5 | UBI+WS | F | 0.5 | WS | P | 1 |
| WS | P | 1 | UBI+WS | F | 0.5 | GMI | F | 0.5 | GMI+WS | P | 0.5 | GMI+WS | P | 0.5 | GMI+WS | P | 0.5 |
| WS | F | 1 | GMI+WS | F | 0.75 | WS | P | 0.75 | WS | P | 0.75 | WS | P | 0.75 | GMI+WS | F | 0.5 |
| WS | P | 0.75 | GMI | F | 0.75 | WS | F | 1 | WS | F | 1 | WS | F | 1 | WS | P | 0.75 |
| GMI+WS | F | 0.5 | GMI+WS | F | 0.5 | GMI+WS | F | 0.5 | GMI+WS | F | 0.5 | GMI+WS | F | 0.5 | WS | F | 1 |
| WS | F | 0.75 | GMI | F | 0.5 | WS | F | 0.75 | WS | F | 0.75 | WS | F | 0.75 |  | NT |  |
| WS | P | 0.5 | WS | F | 1 | WS | P | 0.5 | WS | P | 0.5 | WS | P | 0.5 | WS | P | 0.5 |
| CURRENT |  |  | WS | F | 0.75 | CURRENT |  |  | CURRENT |  |  | CURRENT |  |  | WS | F | 0.75 |
| WS | F | 0.5 | WS | F | 0.5 | WS | F | 0.5 | WS | F | 0.5 | WS | F | 0.5 | WS | F | 0.5 |

Table 3. Effects of policy attributes on Social Welfare. Regression coefficients ( $\boldsymbol{t}$-Statistics in parenthesis)

|  | GSW | PAGSW |
| :--- | ---: | :---: |
| Constant | $94233.08(12.22)$ | $88787.22(70.80)$ |
| Progressive | $12.37(3.37)$ | $457.59(1.32)$ |
| Coverage | $87.22(2.37)$ | $8260.96(2.19)$ |
| Coverage $^{2}$ | $-65.46(-2.48)$ | $-2995.58(-1.11)$ |
| Unconditional | $16.49(4.72)$ | $274.49(0.77)$ |
| Subsidy | $2.16(0.62)$ | $-1944.72(-5.43)$ |

## Note to Table 3

Progressive $=1$ if tax rule is progressive ( 0 otherwise )
Coverage $=$ the value of $a$ as defined in Section 2 (for the CURRENT system we set $a=0.1$ );
Coverage ${ }^{2}=$ Coverage squared;
Unconditional $=1$ if income support mechanism is UBI or UBI+WS (0 otherwise);
Subsidy = 1 if income support mechanism is WS or UBI+WS or GMI+WS ( 0 otherwise).

## Appendix A. Microecometric model, simulation and social evaluation

## A.1. Household behaviour

The basic modelling framework belongs to the family of the Random Utility models and is similar to the one adopted in a series of papers by Aaberge et al. (1995, 1999, 2000, 2004), Dagsvik and Strøm (2006), Aaberge and Colombino (2011) and Colombino et al. (2010). ${ }^{13}$ We will consider households with two decision-makers (couples) or one decision-maker (singles). In both cases the decision-makers are aged 20-55 and are not retired nor students. Of course there might be other people in the household, but their behaviour is taken as exogenous.

A couple $n$ is assumed to solve the following problem

$$
\max _{h_{F}, h_{M}, \varepsilon} U^{n}\left(C, h_{F}, h_{M}, j\right)
$$

(A.1)

$$
\begin{aligned}
& \text { s.t. } \\
& \left(h_{F}, h_{M}, j\right) \in \Omega \\
& C=R\left(w_{F}^{n} h_{F}, w_{M}^{n} h_{M}, y^{n}\right)
\end{aligned}
$$

where
$U^{n}\left(C, h_{F}, h_{M}, j\right)=$ utility function
$h_{g}=$ average weekly hours of work required by the chosen job in the choice set for partner of gender $g=\mathrm{F}$ (female) or M (male);
$w_{g}^{n}=$ hourly wage rate of partner $g$;
$y^{n}=$ vector of exogenous household gross incomes;
$C=$ net disposable household income;
$j=$ unobserved (by the analyst) characteristics of the household-job match;
$\Omega=$ opportunity set containing jobs ( $h_{F}, h_{M}, j$ ), including those with $h_{F}=0$ and/or $h_{M}=0$;
$R=$ tax-transfer rule that transforms gross incomes into net available household income.

The first two constraints of problem (A.1) say that the hours of work $h_{g}$ are chosen within a discrete set of values $A$ including also 0 hours. This discrete set of values can be interpreted as the actual choice set (maybe determined by institutional constraints) or as approximations to the true (possibly continuous) choice set.
The third constraint says that net income $C$ is the result of a tax-transfer rule $R$ applied to gross incomes.

[^9]We write the utility function $U^{n}\left(C, h_{F}, h_{M}, \varepsilon\right)$ as the sum of a parametric systematic part and a random component:

$$
\begin{equation*}
\mathrm{U}^{n}\left(C, h_{F}, h_{M}, j\right)=V\left(R\left(w_{F}^{n} h_{F}, w_{M}^{n} h_{M}, y^{n}\right), h_{F}, h_{M}, Z^{n} ; \theta\right)+\varepsilon(j) \tag{A.2}
\end{equation*}
$$

where $Z^{n}$ is a vector of household characteristics and $\theta$ is a vector of parameters to be estimated. The interpretation of the random variable $\varepsilon$ is analogous to the one given by McFadden in his presentations of the Conditional Logit model (McFadden, 1974): besides the observed variables, there are characteristics of the household-job match that are observed by the household but not by the econometrician; the random variable $\varepsilon$ is meant to account for the contribution to utility by those characteristics.

We denote with $p\left(h_{F}, h_{M}\right)$ the relative frequency (or probability density function) of jobs of type $\left(h_{F}, h_{M}\right) \in \Omega$. The random variable $\varepsilon$ is assumed to be i.i.d. Type I Extreme Value. By specifying $p\left(h_{F}, h_{M}\right)$ as done in Aaberge and Colombino (2011), it turns out that we can write the probability that household $n$ subject to tax-transfer regime $R$ chooses $h_{F}=f, h_{M}=m$ as follows:
(A.3) $P^{n}(f, m ; \theta, R)=\frac{\exp \left\{V\left(R\left(w_{F}^{n} f, w_{M}^{n} m, y^{n}\right), f, m, Z^{n} ; \theta\right)+\sum_{k=1}^{4} \gamma_{F k} D_{F k}(f)+\sum_{k=1}^{4} \gamma_{M k} D_{M k}(m)\right\}}{\sum_{\left(h_{F}, h_{M}\right)} \exp \left\{V\left(R\left(w_{F}^{n} h_{F}, w_{M}^{n} h_{M}, y^{n}\right), h_{F}, h_{M}, Z^{n} ; \theta\right)+\sum_{k=1}^{4} \gamma_{F k} D_{F k}\left(h_{F}\right)+\sum_{k=1}^{4} \gamma_{M k} D_{M k}\left(h_{M}\right)\right\}}$
where

$$
\begin{aligned}
D_{g 1}\left(h_{g}\right) & =\left\{\begin{array}{l}
1 \text { if } 17 \leq h_{g} \leq 32 \\
0 \text { otherwise }
\end{array}\right. \\
D_{g 2}\left(h_{g}\right) & =\left\{\begin{array}{l}
1 \text { if } 33 \leq h_{g} \leq 48 \\
0 \text { otherwise }
\end{array}\right.
\end{aligned}
$$

$$
\begin{align*}
& D_{g 3}\left(h_{g}\right)=\left\{\begin{array}{l}
1 \text { if } 49 \leq h_{g} \\
0 \text { otherwise }
\end{array}\right.  \tag{A.4}\\
& D_{g 4}\left(h_{g}\right)=\left\{\begin{array}{l}
1 \text { if } 0<h_{g} \\
0 \text { otherwise }
\end{array}\right. \\
& \text { with } \mathrm{g}=\mathrm{F} \text { (female) or M (male). }
\end{align*}
$$

In a similar way, a single $s$ of gender $g$ is assumed to solve a constrained utility maximization problem as follows:

$$
\begin{aligned}
& \max _{h, j} U_{g}^{s}(C, h, j) \\
& \text { s.t. } \\
& (h, j) \in \Omega_{g} \\
& C=R\left(w^{s} h, y^{s}\right)
\end{aligned}
$$

where
$h=$ average weekly hours of work required by the chosen job.
In this case, the utility function $U_{g}^{s}(C, h, j)$ will be written as follows:

$$
\begin{equation*}
U_{g}^{s}(C, h ; j)=V\left(R\left(w^{s} h, y^{s}\right), h, Z^{s} ; \theta_{g}\right)+\varepsilon(j) \tag{A.6}
\end{equation*}
$$

Proceeding as we did with couples we end up with:

$$
\begin{equation*}
P^{s}\left(g ; \theta_{g}, \gamma_{g}, R\right)=\frac{\exp \left\{V\left(R\left(w_{g}^{s} g, y^{s}\right), g, Z^{s} ; \theta\right)+\sum_{k=1}^{4} \gamma_{g k} D_{g k}(g)\right\}}{\sum_{h} \exp \left\{V\left(R\left(w_{g}^{s} h, y^{s}\right), h, Z^{s} ; \theta\right)+\sum_{k=1}^{4} \gamma_{g k} D_{g k}(h)\right\}} \tag{A.7}
\end{equation*}
$$

As explained in Aaberge and Colombino (2011) and Colombino (2010), the coefficients of the dummies have the following interpretation, which turn out to be useful for the development of the equilibrium simulation procedure (section A.5):

$$
\begin{align*}
& e^{\gamma_{84}} \propto J_{g} \\
& e^{\gamma_{g k}} \propto J_{g k} / J_{g}, k=1,2,3 \tag{A.8}
\end{align*}
$$

where $J_{g}$ is the number of market jobs in gender g's opportunity set and $J_{g k}$ is the number of jobs with hours h such that

$$
D_{g k}(h)=1 .^{14}
$$

When computing (A.3) and (A.7), the set of hours values is approximated by a discrete set containing the value 0 plus ten values randomly chosen from the ten intervals of weekly hours 1-8, 9-16, 17-24, 25-32, 33-40, 41-48, 49-56, 57-64, 65-$72,73-80$. Therefore the singles' and the couples' opportunity sets contain respectively 11 and 121 alternatives. ${ }^{15}$

In order to compute net household income $C$ for each one of the household jobs contained in $A \times A$, we use the EUROMOD Microsimulation model. ${ }^{16}$ In other words EUROMOD mimics the tax-transfer rule R. Wage rates for those who are observed as not employed are imputed on the basis of a wage equation estimated on the employed subsample and corrected for sample selection.

## A.2. Empirical specification of preferences

We choose a quadratic specification since it is linear-in-parameters and it represents a good compromise between flexibility and ease of estimation:

$$
\begin{align*}
V^{n} & =\theta_{C} C+\theta_{F}\left(T-h_{F}\right)+\theta_{M}\left(T-h_{M}\right)+ \\
& +\theta_{C C} C^{2}+\theta_{F F}\left(T-h_{F}\right)^{2}+\theta_{M M}\left(T-h_{M}\right)^{2}+  \tag{A.6}\\
& +\theta_{C F} C\left(T-h_{M}\right)+\theta_{C M} C\left(T-h_{M}\right)+\theta_{F M}\left(T-h_{F}\right)\left(T-h_{M}\right)
\end{align*}
$$

[^10]\[

$$
\begin{equation*}
V^{s}=\theta_{C} C+\theta_{g}\left(T-h_{g}\right)+\theta_{C C} C^{2}+\theta_{g g}\left(T-h_{g}\right)^{2}+\theta_{C g} C\left(T-h_{g}\right) \tag{A.7}
\end{equation*}
$$

\]

where $V^{n}$ and $V^{s}$ denote the systematic part of the utility function respectively for couples and singles and $T$ denotes total available time.
Some of the above parameters $\theta s$ are made dependent on characteristics:

$$
\begin{aligned}
\theta_{F}= & \beta_{F 0}+\beta_{F 1}(\text { Age of the wife })+\beta_{F 2}(\text { Age of the wife })^{2}+ \\
& +\beta_{F 3}(\# \text { Children })+\beta_{F 4}(\# \text { Children under } 6)+\beta_{F 5}(\# \text { Children } 6-10)
\end{aligned}
$$

$$
\begin{align*}
\theta_{M}= & \beta_{M 0}+\beta_{M 1}(\text { Age of the husband })+\beta_{M 2}(\text { Age of the husband })^{2}+  \tag{A.8}\\
& +\beta_{M 3}(\# \text { Children })+\beta_{M 4}(\# \text { Children under } 6)+\beta_{M 5}(\# \text { Children 6-10 }) \\
\theta_{g}= & \beta_{g 0}+\beta_{g 1}(\text { Age })+\beta_{g 2}(\text { Age })^{2}+\beta_{g 3}(\# \text { Children })+\beta_{g 4}(\# \text { Children under } 6)+\beta_{g 5}(\# \text { Children 6-10 }) \\
\theta_{C}= & \beta_{C 0}+\beta_{C 1}(\text { Household's size }) .
\end{align*}
$$

Notice that the parameters are separately estimated for couples, single females and single males.

## A.3. Estimates

The parameters are estimated by Maximum Likelihood. For the estimation and simulation exercise presented in this paper we use the Italian dataset generated by EUROMOD team from the Survey of Household Income and Wealth (SHIW) 1998.

The inclusion criteria are as follows:

- Couple and single households;
- Employed (self-employed included), unemployed or inactive (students and disabled are excluded);
- Both partners of couple households and heads of single households aged 20-55.

The estimates based on the sample of couples, single men and single women (respectively 2955, 291 and 366 observations) are reported in Table A.1.

The crucial preference parameters are:
$\beta_{C 0}$ and $\theta_{C C}$ (related to the marginal utility of income);
$\beta_{F 0}$ and $\theta_{F F}$ (related to the marginal utility of wife's leisure);
$\beta_{M 0}$ and $\theta_{M M}$ (related to the marginal utility of husband's leisure).
$\beta_{g 0}$ and $\theta_{g g}$ (related to the marginal utility of single household head leisure).
The other parameters $\beta^{\prime} s$ and $\theta^{\prime} s$ measure the effects of various interactions of leisure times and income among themselves and with household characteristics.
The marginal utility of income and the marginal utility of wife's and husband's leisure appear to be positive and decreasing (at least at the observed choices). The wife's and the husband's leisure appear to be complements, in the sense that more leisure of one of them has a positive effect on the marginal utility of leisure of the other one.

Table A.1. Parameter estimates

|  | Couple | Single female | Single Male |
| :---: | :---: | :---: | :---: |
| $\beta_{F 0}$ | . $3301752 * * *$ | . 1562657 |  |
| $\beta_{F 1}$ | $-.0077954 * * *$ | -.0085422* |  |
| $\beta_{F 2}$ | . $0001051^{* * *}$ | .0001062* |  |
| $\beta_{F 3}$ | . $0086118 * * *$ | . 0097963 |  |
| $\beta_{F 4}$ | -. 0018444 | -. 0025955 |  |
| $\beta_{F 5}$ | . 0030899 | . 0130587 |  |
| $\beta_{M 0}$ | . 0338491 |  | .2237299* |
| $\beta_{M 1}$ | . 001687 |  | -. 0053004 |
| $\beta_{M 2}$ | -. 0000218 |  | . 0000694 |
| $\beta_{M 3}$ | . 0035718 |  | -. 0685087 |
| $\beta_{M 4}$ | $-.0105606^{* * *}$ |  | . 0614548 |
| $\beta_{M 5}$ | $-.0077151^{* *}$ |  | . 0634671 |
| $\beta_{C 0}$ | . $0004311 * * *$ | -. 0001394 | . 0002968 |
| $\beta_{C 1}$ | -. 00000251 | . 0000433 | -. 00006642 |
| $\theta_{C C}$ | -9.12e-09* | -1.42e-08 | -8.87e-09 |
| $\theta_{\text {FF }}$ | $-.0008251^{* * *}$ | .0008978* |  |
| $\theta_{M M}$ | .0003973** |  | -. 00000417 |
| $\theta_{\text {CF }}$ | -1.92e-06* | 5.70e-06 |  |

Table A.1. Parameter estimates (cont'd)

|  | Couple | Single female | Single Male |
| :---: | :---: | :---: | :---: |
| $\theta_{C M}$ | -1.01e-06 |  | -1.23e-06 |
| $\theta_{F M}$ | .0001992* |  |  |
| $\gamma_{F 1}$ | $3.07818^{* * *}$ | 4.069606*** |  |
| $\gamma_{F 2}$ | $5.223014^{* * *}$ | 7.077753*** |  |
| $\gamma_{\text {F3 }}$ | $5.260581 * * *$ | $6.363261^{* * *}$ |  |
| $\gamma_{F 4}$ | $-3.356024^{* * *}$ | $-1.131054 * *$ |  |
| $\gamma_{M 1}$ | $3.673685^{* * *}$ |  | $2.997396 * * *$ |
| $\gamma_{M 2}$ | 8.314315*** |  | 6.786832*** |
| $\gamma_{M 3}$ | $8.917805^{* * *}$ |  | 7.232927*** |
| $\gamma_{M 4}$ | $-.8084671^{* * *}$ |  | -. 7926529 |

For the meaning of the coefficient symbols see expressions A.6, A.7, A. 8 and A.10.
$* * *=$ significance $<1 \%$
$* *=$ significance $<5 \%$

* $=$ significance $<10 \%$


## A.4. Behavioural simulation method

The estimated model is used to simulate the effects of alternative hypothetical tax-transfer reforms upon variables such as the number of employed, the taxes paid etc. There are many possible methods that can be used to compute these predictions. We adopt the method of computing the expected value. Let $P^{n}(f, m ; \theta, \gamma, R)$ be the probability that household $n$ chooses $(f, m)$ under the $R$ tax-transfer regime, computed on the basis of the estimated parameters. Suppose we are interested in simulating the expected value of some function $\psi^{n}(f, m)$ of the choices made. Then we compute the expected value of that variable after the policy is implemented as follows:

$$
\begin{equation*}
E\left(\psi^{n}(f, m)\right)=\sum_{(f, m) \in \Omega} \psi^{n}(f, m) P^{n}\left(f, m, Z^{n} ; \theta, \gamma, R\right) . \tag{A.11}
\end{equation*}
$$

An analogous procedure is for singles.

## A.5. Simulation under equilibrium

The microeconometric model adopts the widely used refinement consisting of introducing alternative-specific constants, which should account for a number of factors such as the different density or accessibility of different types of jobs, search or fixed costs and systematic utility components otherwise not accounted for (expression A.10). Many papers have adopted a similar procedure, e.g.: Van Soest (1995), Aaberge et al. (1995, 1999, 2000, 2004), Aaberge and Colombino (2011, 2012), Kalb (2000), Dagsvik and Strøm (2006), Kornstad et al. (2007) and Colombino et al. (2010). All the authors adopting the "dummies refinement" so far have performed the simulations while leaving the dummies' coefficients $\gamma$ 's unchanged. The policy simulation is most commonly interpreted as a comparative statics exercise, where different equilibria - induced by different tax-transfer regimes - are compared. We claim that the standard procedure in general is not consistent with the comparative statics interpretation. According to a basic notion of equilibrium, the number of people willing to work must equal to the number of available jobs. Since the $\gamma$ 's reflect - at least in part - the number and the composition of available jobs (expression A.8), and since the number of people willing to work and their distribution across different job types in general change as a consequence of the reforms, it follows that in general the $\gamma$ 's must also change. Building on a matching model developed by Dagsvik $(1994,2000)$ we can extend the basic random utility approach to include a random choice set and provide a structural interpretation of the "dummies refinement" that leads very naturally to a simulation procedure consistent with comparative statics. ${ }^{17}$ The procedure is explained in Colombino (2010) and requires to adjust the $\gamma$ 's so that an appropriate equilibrium condition is fulfilled.

[^11]
## A.6. Social evaluation

In section 3 of the main text we define two Social Welfare functions. Their computation requires the following steps.

1) Expected maximum utility attained by household $n$ under tax-transfer regime $R:{ }^{18}$
(A.12)

$$
V^{n}(R)=\left\{\begin{array}{l}
\ln \left(\sum_{\left(h_{F}, h_{M}\right)} \exp \left\{V\left(R\left(w_{F}^{n} h_{F}, w_{M}^{n} h_{M}, y^{n}\right), h_{F}, h_{M}, Z^{n} ; \theta, \gamma\right)+\sum_{k=1}^{5} \gamma_{F k} D_{F k}\left(h_{F}\right)+\sum_{k=1}^{5} \gamma_{F k} D_{M k}\left(h_{M}\right)\right\}\right) \\
\text { if couple } \\
\ln \left(\sum_{h} \exp \left\{V\left(R\left(w^{n} h, y^{n}\right), h, Z^{n} ; \theta, \gamma\right)+\sum_{k=1}^{5} \gamma_{k} D_{k}(h)+\sum_{k=1}^{5} \gamma_{k} D_{k}(h)\right\}\right) \\
\text { if single }
\end{array}\right.
$$

2) Interpersonally-comparable-metric utility ${ }^{19}$ of household $i$ under tax regime $R, \mu_{i}(R)$.

Let $V^{0}\left(R_{0}\right)$ be the expected maximum utility attained by a reference household under a reference tax-transfer regime. In this paper we choose as reference household the poorest single in 1998 and as reference tax-transfer system the 1998 system:

$$
\begin{equation*}
V^{0}\left(R_{0}\right)=\ln \left(\sum_{h} \exp \left\{V\left(R_{0}\left(w^{0} h, y^{0}\right), h, Z^{0} ; \theta, \gamma\right)+\sum_{k=1}^{4} \gamma_{k} D_{k}(h)\right\}\right) \tag{A.13}
\end{equation*}
$$

The interpersonally-comparable money-metric utility of household $n$ under tax regime $R, \mu^{n}(R)$, is then defined by:

$$
\begin{equation*}
\ln \left(\sum_{h} \exp \left\{V\left(\mu^{n}(R), h, Z^{0} ; \theta, \gamma\right)+\sum_{k=1}^{4} \gamma_{k} D_{k}(h)\right\}\right)=V^{n}(R) . \tag{A.14}
\end{equation*}
$$

In other words, $\mu^{n}(R)$ is the net available income needed by the reference household under the reference tax-transfer regime in order to attain the same expected maximum utility level of household $n$ under tax-transfer regime $R$.
3) Expressions (A.12) - (A.14) assume that the household is able to choose the constrained utility-maximizing "job". In the Non-behavioural simulation this assumption is not appropriate anymore. The procedure we adopt is explained hereafter; it is referred to single households, the extension to couples is immediate.

Let
$h_{1998}^{n}=$ hours of work of household $n$ under the 1998 regime,
$h_{1998}^{0}=$ hours of work of the reference household under the 1998 regime.
Then $\mu^{n}(R)$ is defined by:

$$
\begin{equation*}
V\left(\mu^{n}(R), h_{1998}^{0}, Z^{0} ; \theta, \gamma\right)=V\left(R\left(w^{n} h_{1998}^{0}, y^{n}\right), h_{1998}^{0}, Z^{n} ; \theta, \gamma\right) \tag{A.15}
\end{equation*}
$$

[^12]4) The Gini Social Welfare (GSW) function and the Poverty-adjusted Social Welfare (PAGSW) function are computed as follows:
$$
G S W(R)=\mu(R)(1-I(R))
$$
(A.16)
$$
\operatorname{PAGSW}(R)=\mu(R)(1-I(R)-p(R))
$$
where:
$\mu(R)=\frac{1}{N} \sum_{n} \mu^{n}(R)$
$I(R)=$ Gini coefficient of the sample distribution of $\mu_{n}(R)$
$p(R)=$ head-count poverty ratio.

## Appendix B. The reforms

Tables B. 1 and B. 2 specify net available income as a function of taxable income under the reforms.
Definitions:
$x_{F}=w_{F} h_{F}=$ female gross earnings; $x_{M}=w_{M} h_{M}=$ male gross earnings; $x=x_{F}+x_{M}$
$y_{F}=$ female unearned gross income; $y_{M}=$ male unearned gross income
$m=$ other household net income
$S_{F}=$ social security contributions (female); $S_{M}=$ social security contributions (male); $S=S_{F}+S_{M}$
$I_{F}=g_{F}+y_{F}-S_{F}=$ taxable income (female) $; I_{M}=g_{M}+y_{M}-S_{M}=$ taxable income (male) $; I=I_{F}+I_{M}$
$P=$ poverty line
$N=$ number of people in the household
$G=\alpha P \sqrt{N}$ with $\alpha=1,0.75,0.50$ (defined Section 2)
$C_{F}=$ net available income (female); $C_{M}=$ net disposable income (male); $C=m+C_{F}+C_{M}$
$T=$ taxes paid by the household
$B=$ benefits or transfers received by household
$\mathrm{q}=$ average propensity to consumption
$r=$ average VAT rate
$\omega=$ proportional subsidy on the gross wage rate
$\varphi()=$. progressive tax function
The current (1998) marginal tax rates are as follows:
Income Brackets Marginal Tax Rates

| $0-7.7$ | 18 |
| :---: | :---: |
| $7.7-15.5$ | 26 |
| $15.5-31$ | 33 |
| $31-69.7$ | 39 |
| $>69.7$ | 45 |

Income brackets (originally in Italian Lire) are expressed in thousands of Euros.
Under the 1998 system the above rates are applied to personal earnings, together with deductions, allowances and benefits. Under the reforms all deductions, tax credits and benefits are cancelled, the income brackets are kept unchanged and the marginal tax rates (either the flat or the progressive ones) are applied to the whole personal income (not just to earnings).

Public Budget Constraint: $\sum T^{1}-\sum B^{1}+r \sum q C^{1}+\sum S^{1}=\sum T^{0}-\sum B^{0}+r \sum q C^{0}+\sum S^{0}$
where the superscript R denotes a generic reform and the superscript 0 denotes the current system.

Table B.1. Net available income as a function of taxable income - Couples

|  | Flat | Progressive |
| :---: | :---: | :---: |
| GMI | $\begin{aligned} & C_{F}=\left\{\begin{array}{l} G / 2 \text { if } I_{F} \leq G / 2 \\ G / 2+\left(I_{F}-G / 2\right)(1-t) \text { if } I_{F}>G / 2 \end{array}\right. \\ & C_{M}=\left\{\begin{array}{l} G / 2 \text { if } I_{M} \leq G / 2 \\ G / 2+\left(I_{M}-G / 2\right)(1-t) \text { if } I_{M}>G / 2 \end{array}\right. \end{aligned}$ | $\begin{aligned} & C_{F}=\left\{\begin{array}{l} G / 2 \text { if } I_{F} \leq G / 2 \\ G / 2+\varphi\left(I_{F}-G / 2\right) \text { if } I_{F}>G / 2 \end{array}\right. \\ & C_{M}=\left\{\begin{array}{l} G / 2 \text { if } I_{M} \leq G / 2 \\ G / 2+\varphi\left(I_{M}-G / 2\right) \text { if } I_{M}>G / 2 \end{array}\right. \end{aligned}$ |
| UBI | $\begin{aligned} & C_{F}=G / 2+I_{M}(1-t) \\ & C_{M}=G / 2+I_{M}(1-t) \end{aligned}$ | $\begin{aligned} & C_{F}=G / 2+\varphi\left(I_{F}\right) \\ & C_{M}=G / 2+\varphi\left(I_{M}\right) \end{aligned}$ |
| WS | $\begin{aligned} & C_{F}=\left\{\begin{array}{l} \left(I_{F}+\omega x_{F}\right) \text { if }\left(I_{F}+\omega x_{F}\right) \leq G / 2 \\ G / 2+\left(\left(I_{F}+\omega x_{F}\right)-G / 2\right)(1-t) \text { if }\left(I_{F}+\omega x_{F}\right)>G / 2 \end{array}\right. \\ & C_{s}=\left\{\begin{array}{l} \left(I_{\mu}+\omega x_{\mu}\right) \text { if }\left(I_{s}+\omega x_{s}\right) \leq G / 2 \\ G / 2+\left(\left(I_{M}+\omega x_{M}\right)-G / 2\right)(1-t) \text { if }\left(I_{M}+\omega x_{s}\right)>G / 2 \end{array}\right. \end{aligned}$ | $\begin{aligned} & C_{F}=\left\{\begin{array}{l} \left(I_{F}+\omega x_{F}\right) \text { if }\left(I_{F}+\omega x_{F}\right) \leq G / 2 \\ G / 2+\varphi\left(\left(I_{F}+\omega x_{F}\right)-G / 2\right) \text { if }\left(I_{F}+\omega x_{F}\right)>G / 2 \end{array}\right. \\ & C_{M}=\left\{\begin{array}{l} \left(I_{M}+\omega x_{M}\right) \text { if }\left(I_{M}+\omega x_{M}\right) \leq G / 2 \\ G / 2+\varphi\left(\left(I_{M}+\omega x_{M}\right)-G / 2\right) \text { if }\left(I_{M}+\omega x_{M}\right)>G / 2 \end{array}\right. \end{aligned}$ |
| GMI+WS | $\begin{aligned} & C_{F}=\left\{\begin{array}{l} 0.5 G / 2 \text { if }\left(I_{F}+\omega x_{\digamma}\right) \leq 0.5 G / 2 \\ \left(I_{F}+\omega x_{r}\right) \text { if } 0.5 G / 2<\left(I_{F}+\omega x_{r}\right) \leq G / 2 \\ G / 2+\left(\left(I_{F}+\omega x_{r}\right)-G / 2\right)(1-t) \text { if }\left(I_{F}+\omega x_{r}\right)>G / 2 \end{array}\right. \\ & C_{\mu}=\left\{\begin{array}{l} 0.5 G / 2 \text { if }\left(I_{s}+\omega x_{\mu}\right) \leq 0.5 G / 2 \\ \left(I_{\mu}+\omega x_{\mu}\right) \text { if } 0.5 G / 2<\left(I_{\mu}+\omega x_{\mu}\right) \leq G / 2 \\ G / 2+\left(\left(I_{\mu}+\omega x_{\mu}\right)-G / 2\right)(1-t) \text { if }\left(I_{\mu}+\omega x_{\mu}\right)>G / 2 \end{array}\right. \end{aligned}$ | $\begin{aligned} & C_{F}=\left\{\begin{array}{l} 0.5 G / 2 \text { if }\left(I_{F}+\omega x_{F}\right) \leq 0.5 G / 2 \\ \left(I_{F}+\omega x_{F}\right) \text { if } 0.5 G / 2<\left(I_{F}+\omega x_{F}\right) \leq G / 2 \\ G / 2+\varphi\left(\left(I_{F}+\omega x_{F}\right)-G / 2\right) \text { if }\left(I_{F}+\omega x_{F}\right)>G / 2 \end{array}\right. \\ & C_{M}=\left\{\begin{array}{l} 0.5 G / 2 \text { if }\left(I_{M}+\omega g_{M}\right) \leq 0.5 G / 2 \\ \left(I_{M}+\omega x_{M}\right) \text { if } 0.5 G / 2<\left(I_{M}+\omega x_{M}\right) \leq G / 2 \\ G / 2+\varphi\left(\left(I_{M}+\omega x_{M}\right)-G / 2\right) \text { if }\left(I_{M}+\omega x_{M}\right)>G / 2 \end{array}\right. \end{aligned}$ |
| UBI+WS | $\begin{aligned} C_{F} & =\left\{\begin{array}{l} 0.5 G / 2+\left(\mathrm{I}_{F}+w x_{F}\right) \text { if }\left(\mathrm{I}_{F}+w x_{F}\right) \leq 0.5 G / 2 \\ 0.5 G / 2+\left(I_{F}+w x_{F}\right)(1-t) \text { if }\left(I_{F}+w x_{F}\right)>0.5 G / 2 \end{array}\right. \\ C_{M} & =\left\{\begin{array}{l} 0.5 G / 2+\left(\mathrm{I}_{M}+w x_{M}\right) \text { if }\left(\mathrm{I}_{M}+w x_{M}\right) \leq 0.5 G / 2 \\ 0.5 G / 2+\left(I_{M}+w x_{M}\right)(1-t) \text { if }\left(I_{M}+w x_{M}\right)>0.5 G / 2 \end{array}\right. \end{aligned}$ | $\begin{aligned} C_{F} & =\left\{\begin{array}{l} 0.5 G / 2+\left(\mathrm{I}_{F}+w x_{F}\right) \text { if }\left(\mathrm{I}_{F}+w x_{F}\right) \leq 0.5 G / 2 \\ 0.5 G / 2+\varphi\left(I_{F}+w x_{F}\right) \text { if }\left(I_{F}+w x_{F}\right)>0.5 G / 2 \end{array}\right. \\ C_{M} & =\left\{\begin{array}{l} 0.5 G / 2+\left(\mathrm{I}_{M}+w x_{M}\right) \text { if }\left(\mathrm{I}_{M}+w x_{M}\right) \leq 0.5 G / 2 \\ 0.5 G / 2+\varphi\left(I_{M}+w x_{M}\right) \text { if }\left(I_{M}+w x_{M}\right)>0.5 G / 2 \end{array}\right. \end{aligned}$ |

Table B.2. Net available income as a function of taxable income - Singles

|  | Flat | Progressive |
| :---: | :---: | :---: |
| GMI | $C=\left\{\begin{array}{l}G \text { if } I \leq G \\ G+(I-G)(1-t) \text { if } I>G\end{array}\right.$ | $C=\left\{\begin{array}{l}G \text { if } I \leq G \\ G+\varphi(I-G) \text { if } I>G\end{array}\right.$ |
| UBI | $C=G+I(1-t)$ | $C=G+\varphi(I)$ |
| WS | $C=\left\{\begin{array}{l} (I+\omega x) \text { if }(I+\omega x) \leq G \\ G+((I+\omega x)-G)(1-t) \text { if }(I+\omega x)>G / 2 \end{array}\right.$ | $C=\left\{\begin{array}{l}(I+\omega x) \text { if }(I+\omega x) \leq G \\ G+\varphi((I+\omega x)-G) \text { if }(I+\omega x)>G\end{array}\right.$ |
| GMI+WS | $C=\left\{\begin{array}{l} 0.5 G \text { if }(I+\omega x) \leq 0.5 G \\ (I+\omega x) \text { if } 0.5 G<(I+\omega x) \leq G \\ G+((I+\omega x)-G)(1-t) \text { if }(I+\omega x)>G \end{array}\right.$ | $C=\left\{\begin{array}{l} 0.5 G \text { if }(I+\omega x) \leq 0.5 G \\ (I+\omega x) \text { if } 0.5 G<(I+\omega x) \leq G \\ G+\varphi((I+\omega x)-G) \text { if }(I+\omega x)>G \end{array}\right.$ |
| UBI+WS | $C=\left\{\begin{array}{l} 0.5 G+(\mathrm{I}+w x) \text { if }(\mathrm{I}+w x) \leq 0.5 G \\ 0.5 G+(I+w x)(1-t) \text { if }(I+w x)>0.5 G \end{array}\right.$ | $C=\left\{\begin{array}{l} 0.5 G+(\mathrm{I}+w x) \text { if }(\mathrm{I}+w x) \leq 0.5 G \\ 0.5 G+\varphi\left(I_{F}+w x_{F}\right) \text { if }\left(I_{F}+w x_{F}\right)>0.5 G \end{array}\right.$ |

## Appendix C. Behavioural, fiscal and welfare effects of the reforms

## Legenda for Tables C. 1 - C. 6

(a) = either the CURRENT tax-transfer rule or a reform: the first label refers to the income support mechanism, the second label denotes flat $(\mathrm{F})$ or progressive $(\mathrm{P})$ marginal tax rates, the last number is the guaranteed minimum income as a proportion of the poverty line.
(b): average male weekly expected hours of work (including the 0 hours of non participants).
(c): average female weekly expected hours of work (including the 0 hours of non participants).
(d): average monthly gross income (Euros 1998).
(e): average monthly net available income (Euros 1998).
(f): for Flat tax rules, it is the constant tax rates; for Progressive tax rules, it is the proportional increase with respect to the current marginal rates (reported in Appendix B).
(g): average monthly benefit (transfer + wage subsidy) received by the household (Euros 1998).
(h): proportion of utility-winners (household $n$ is a utility-winner under reform $R_{1}$ with respect to the current system $R_{0}$ if $\mu^{n}\left(R_{1}\right)>\mu^{n}\left(R_{0}\right)-$ see section 4).
(i): proportion of income-winners (a household is a income-winner if household's net available income is higher under the reform than under the current system).
(1): poverty ratio (head-count rate) = number of poor as a percentage of the number of households in the sample.
$(\mathrm{m})$ : poverty-gap ratio $=$ average distance between the poverty line and the incomes of the poor, as a percentage of the poverty line.
$(\mathrm{n})$ : income-gap ratio $=$ distance between the poverty line and the average income of the poor, as a percentage of the poverty line.
(o): Gini Social Welfare.
(p): Poverty-adjusted Gini Social Welfare.

Table C.1. No Behaviour

| a) |  |  | (b) | (c) | (d) | (e) | (f) | (g) | (h) | (i) | (1) | (m) | (n) | (o) | (p) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | 0 <br> 0 <br> 0 <br> $\ddot{0}$ |  |  |  | $\begin{aligned} & 0.0 \\ & 0 \\ & 0 \\ & =0 \\ & =0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { 気 } \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  |  | 苞 | $\begin{aligned} & 3 \\ & 0 \\ & 2 \\ & 2 \end{aligned}$ |
| CURRENT |  |  | 39.35 | 19.45 | 2930 | 2191 | -- | 101 | -- | -- | 4.23 | 0.58 | 13.71 | 81466 | 77829 |
| GMI | F | 0.5 | 39.35 | 19.45 | 2930 | 2194 | 0.31 | 192 | 0.38 | 0.57 | 2.95 | 0.31 | 10.51 | 81449 | 78911 |
| GMI | F | 0.75 | 39.35 | 19.45 | 2930 | 2196 | 0.37 | 265 | 0.37 | 0.60 | 0.97 | 0.06 | 6.50 | 81451 | 80619 |
| GMI | F | 1 | 39.35 | 19.45 | 2930 | 2201 | 0.45 | 349 | 0.41 | 0.58 | 0.01 | 0.00 | 0.81 | 81452 | 81447 |
| GMI | P | 0.5 | 39.34 | 19.45 | 2930 | 2191 | 0.02 | 192 | 0.52 | 0.63 | 2.38 | 0.25 | 10.63 | 81469 | 79427 |
| GMI | P | 0.75 | 39.34 | 19.45 | 2930 | 2192 | 0.07 | 265 | 0.49 | 0.60 | 0.87 | 0.06 | 6.69 | 81468 | 80723 |
| GMI | P | 1 | 39.33 | 19.45 | 2930 | 2195 | 0.13 | 349 | 0.47 | 0.60 | 0.02 | 0.00 | 1.12 | 81467 | 81448 |
| GMI+WS | F | 0.5 | 39.35 | 19.45 | 2930 | 2197 | 0.36 | 405 | 0.46 | 0.58 | 3.82 | 0.50 | 13.06 | 81457 | 78175 |
| GMI+WS | F | 0.75 | 39.35 | 19.45 | 2930 | 2198 | 0.40 | 435 | 0.48 | 0.62 | 2.65 | 0.28 | 10.49 | 81463 | 79189 |
| GMI+WS | F | 1 | 39.35 | 19.45 | 2930 | 2200 | 0.45 | 467 | 0.51 | 0.64 | 1.53 | 0.12 | 8.11 | 81469 | 80151 |
| GMI+WS | P | 0.5 | 39.35 | 19.45 | 2930 | 2187 | 0.06 | 405 | 0.61 | 0.63 | 3.25 | 0.41 | 12.63 | 81478 | 78686 |
| GMI+WS | P | 0.75 | 39.35 | 19.45 | 2930 | 2183 | 0.09 | 435 | 0.59 | 0.61 | 2.40 | 0.26 | 10.65 | 81478 | 79418 |
| GMI+WS | P | 1 | 39.35 | 19.45 | 2930 | 2179 | 0.13 | 467 | 0.57 | 0.59 | 1.46 | 0.13 | 9.15 | 81479 | 80226 |
| UBI | F | 0.5 | 39.35 | 19.45 | 2930 | 2205 | 0.41 | 568 | 0.53 | 0.63 | 0.91 | 0.06 | 6.95 | 81474 | 80693 |
| UBI | F | 0.75 | 39.35 | 19.45 | 2930 | 2210 | 0.50 | 814 | 0.53 | 0.60 | 0.08 | 0.00 | 2.80 | 81480 | 81413 |
| UBI | F | 1 | 39.35 | 19.45 | 2930 | 2214 | 0.60 | 1060 | 0.53 | 0.60 | 0.00 | 0.00 | 0.00 | 81480 | 81480 |
| UBI | P | 0.5 | 39.35 | 19.45 | 2930 | 2204 | 0.13 | 568 | 0.62 | 0.63 | 0.60 | 0.04 | 6.34 | 81493 | 80979 |
| UBI | P | 0.75 | 39.35 | 19.45 | 2930 | 2209 | 0.22 | 814 | 0.59 | 0.63 | 0.04 | 0.00 | 3.36 | 81494 | 81464 |
| UBI | P | 1 | 39.35 | 19.45 | 2930 | 2213 | 0.32 | 1060 | 0.56 | 0.62 | 0.00 | 0.00 | 0.00 | 81490 | 81490 |
| UBI+WS | F | 0.5 | 39.35 | 19.45 | 2930 | 2200 | 0.38 | 598 | 0.50 | 0.61 | 3.29 | 0.38 | 11.64 | 81463 | 78631 |
| UBI+WS | F | 0.75 | 39.35 | 19.45 | 2930 | 2203 | 0.42 | 721 | 0.53 | 0.64 | 1.96 | 0.17 | 8.84 | 81469 | 79786 |
| UBI+WS | F | 1 | 39.35 | 19.45 | 2930 | 2206 | 0.47 | 844 | 0.53 | 0.63 | 0.83 | 0.05 | 5.92 | 81475 | 80761 |
| UBI+WS | P | 0.5 | 39.35 | 19.45 | 2930 | 2201 | 0.10 | 598 | 0.68 | 0.67 | 2.46 | 0.24 | 9.88 | 81489 | 79373 |
| UBI+WS | P | 0.75 | 39.35 | 19.45 | 2930 | 2205 | 0.14 | 721 | 0.66 | 0.65 | 1.15 | 0.08 | 7.08 | 81494 | 80505 |
| UBI+WS | P | 1 | 39.35 | 19.45 | 2930 | 2210 | 0.18 | 844 | 0.64 | 0.64 | 0.33 | 0.01 | 4.40 | 81501 | 81218 |
| WS | F | 0.5 | 39.35 | 19.45 | 2930 | 2201 | 0.34 | 352 | 0.51 | 0.57 | 4.59 | 0.75 | 16.29 | 81462 | 77518 |
| WS | F | 0.75 | 39.35 | 19.45 | 2930 | 2203 | 0.36 | 352 | 0.57 | 0.62 | 4.05 | 0.60 | 14.92 | 81469 | 77988 |
| WS | F | 1 | 39.35 | 19.45 | 2930 | 2205 | 0.39 | 352 | 0.62 | 0.64 | 3.55 | 0.49 | 13.86 | 81477 | 78420 |
| WS | P | 0.5 | 39.35 | 19.45 | 2930 | 2191 | 0.04 | 352 | 0.65 | 0.64 | 4.12 | 0.63 | 15.30 | 81483 | 77939 |
| WS | P | 0.75 | 39.35 | 19.45 | 2930 | 2189 | 0.05 | 352 | 0.67 | 0.64 | 3.69 | 0.55 | 14.98 | 81487 | 78312 |
| WS | P | 1 | 39.35 | 19.45 | 2930 | 2186 | 0.07 | 352 | 0.69 | 0.64 | 3.39 | 0.48 | 14.29 | 81491 | 78574 |

Table C.2. No Equilibrium

| a) |  |  | (b) | (c) | (d) | (e) | (f) | (g) | (h) | (i) | (1) | (m) | (n) | (o) | (p) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & . \\ & \vdots \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  |  |  | 跴 |  | \% \# \# 0 0 |  |  | 各 | $\begin{aligned} & 3 \\ & 2 \\ & 2 \\ & 2 \end{aligned}$ |
| CURRENT |  |  | 39.35 | 19.45 | 2930 | 2191 | -- | 101 | -- | -- | 4.23 | 0.58 | 13.71 | 94255 | 86391 |
| GMI | F | 0.5 | 39.32 | 19.22 | 2925 | 2190 | 0.31 | 194 | 0.39 | 0.56 | 2.97 | 0.31 | 10.58 | 94241 | 86375 |
| GMI | F | 0.75 | 39.28 | 19.07 | 2912 | 2183 | 0.38 | 269 | 0.37 | 0.55 | 0.93 | 0.06 | 6.39 | 94244 | 863835 |
| GMI | F | 1 | 39.23 | 18.91 | 2896 | 2176 | 0.46 | 357 | 0.40 | 0.53 | 0.00 | 0.00 | 0.16 | 94248 | 86394 |
| GMI | P | 0.5 | 39.31 | 19.24 | 2922 | 2185 | 0.02 | 194 | 0.52 | 0.62 | 2.36 | 0.25 | 10.55 | 94259 | 86393 |
| GMI | P | 0.75 | 39.27 | 19.08 | 2909 | 2176 | 0.07 | 269 | 0.47 | 0.57 | 0.87 | 0.05 | 6.22 | 94259 | 86397 |
| GMI | P | 1 | 39.22 | 18.91 | 2892 | 2168 | 0.14 | 357 | 0.45 | 0.55 | 0.01 | 0.00 | 0.66 | 94259 | 86404 |
| GMI+WS | F | 0.5 | 39.34 | 19.38 | 2932 | 2198 | 0.36 | 406 | 0.47 | 0.59 | 3.90 | 0.51 | 13.11 | 94248 | 86380 |
| GMI+WS | F | 0.75 | 39.32 | 19.31 | 2926 | 2195 | 0.40 | 435 | 0.49 | 0.61 | 2.69 | 0.28 | 10.40 | 94253 | 86387 |
| GMI+WS | F | 1 | 39.30 | 19.24 | 2919 | 2191 | 0.45 | 467 | 0.50 | 0.60 | 1.38 | 0.12 | 8.68 | 94260 | 86394 |
| GMI+WS | P | 0.5 | 39.33 | 19.39 | 2930 | 2187 | 0.06 | 405 | 0.60 | 0.63 | 3.26 | 0.41 | 12.63 | 94267 | 86393 |
| GMI+WS | P | 0.75 | 39.31 | 19.32 | 2923 | 2177 | 0.09 | 435 | 0.58 | 0.59 | 2.34 | 0.25 | 10.64 | 94268 | 86392 |
| GMI+WS | P | 1 | 39.29 | 19.24 | 2915 | 2167 | 0.13 | 467 | 0.56 | 0.56 | 1.43 | 0.13 | 8.96 | 94270 | 86391 |
| UBI | F | 0.5 | 39.28 | 19.22 | 2915 | 2192 | 0.41 | 568 | 0.51 | 0.59 | 0.86 | 0.06 | 6.84 | 94265 | 86404 |
| UBI | F | 0.75 | 39.23 | 19.06 | 2897 | 2183 | 0.51 | 814 | 0.51 | 0.56 | 0.06 | 0.00 | 2.91 | 94271 | 86415 |
| UBI | F | 1 | 39.17 | 18.90 | 2876 | 2172 | 0.61 | 1060 | 0.50 | 0.55 | 0.00 | 0.00 | 0.00 | 94272 | 86420 |
| UBI | P | 0.5 | 39.27 | 19.23 | 2907 | 2185 | 0.13 | 568 | 0.60 | 0.60 | 0.52 | 0.04 | 6.73 | 94283 | 86422 |
| UBI | P | 0.75 | 39.21 | 19.06 | 2885 | 2173 | 0.23 | 814 | 0.56 | 0.58 | 0.04 | 0.00 | 2.52 | 94285 | 86428 |
| UBI | P | 1 | 39.15 | 18.89 | 2859 | 2158 | 0.33 | 1060 | 0.54 | 0.57 | 0.00 | 0.00 | 0.00 | 94280 | 86428 |
| UBI+WS | F | 0.5 | 39.33 | 19.36 | 2930 | 2200 | 0.38 | 598 | 0.51 | 0.61 | 3.30 | 0.40 | 12.04 | 94253 | 86389 |
| UBI+WS | F | 0.75 | 39.31 | 19.28 | 2922 | 2196 | 0.43 | 720 | 0.52 | 0.62 | 1.96 | 0.17 | 8.78 | 94260 | 86398 |
| UBI+WS | F | 1 | 39.28 | 19.21 | 2914 | 2193 | 0.47 | 843 | 0.51 | 0.60 | 0.73 | 0.05 | 6.25 | 94266 | 86407 |
| UBI+WS | P | 0.5 | 39.32 | 19.38 | 2924 | 2196 | 0.10 | 597 | 0.66 | 0.66 | 2.44 | 0.24 | 9.75 | 94279 | 86414 |
| UBI+WS | P | 0.75 | 39.29 | 19.30 | 2914 | 2193 | 0.14 | 719 | 0.64 | 0.62 | 1.01 | 0.07 | 7.43 | 94285 | 86422 |
| UBI+WS | P | 1 | 39.26 | 19.22 | 2903 | 2189 | 0.19 | 842 | 0.61 | 0.61 | 0.17 | 0.01 | 6.80 | 94292 | 86430 |
| WS | F | 0.5 | 39.36 | 19.49 | 2921 | 2205 | 0.34 | 352 | 0.52 | 0.58 | 4.67 | 0.76 | 16.29 | 91925 | 85178 |
| WS | F | 0.75 | 39.36 | 19.50 | 2919 | 2207 | 0.36 | 352 | 0.57 | 0.63 | 4.16 | 0.62 | 14.87 | 91933 | 85186 |
| WS | F | 1 | 39.35 | 19.50 | 2918 | 2208 | 0.39 | 352 | 0.62 | 0.65 | 3.56 | 0.50 | 13.91 | 91941 | 85194 |
| WS | P | 0.5 | 39.36 | 19.53 | 2922 | 2197 | 0.04 | 352 | 0.65 | 0.65 | 4.11 | 0.64 | 15.48 | 94272 | 86400 |
| WS | P | 0.75 | 39.35 | 19.52 | 2920 | 2193 | 0.05 | 352 | 0.68 | 0.65 | 3.67 | 0.55 | 15.01 | 94276 | 86401 |
| WS | P | 1 | 39.35 | 19.53 | 2918 | 2189 | 0.07 | 352 | 0.69 | 0.64 | 3.38 | 0.48 | 14.21 | 94280 | 86402 |

## Table C.3. Equilibrium: $\boldsymbol{\eta}=\mathbf{0}$

| (a) |  |  | (b) | (c) | (d) | (e) | (f) | (g) | (h) | (i) | (1) | (m) | (n) | (o) | (p) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | 0 0 0 0 0 0 0 0 |  |  |  | 首卷 |  | O 0 0 0 |  |  | $3$ | $\begin{aligned} & 3 \\ & 0 \\ & 2 \\ & 2 \end{aligned}$ |
| CURRENT |  |  | 39.35 | 19.45 | 2930 | 2191 | -- | 101 | -- | -- | 4.23 | 0.58 | 13.71 | 94255 | 90047 |
| GMI | F | 0.5 | 39.39 | 19.50 | 3193 | 2433 | 0.29 | 191 | 0.83 | 0.91 | 3.60 | 0.40 | 10.98 | 94324 | 90745 |
| GMI | F | 0.75 | 39.38 | 19.47 | 3306 | 2533 | 0.33 | 260 | 0.88 | 0.95 | 1.81 | 0.15 | 8.13 | 94363 | 92561 |
| GMI | F | 1 | 39.36 | 19.38 | 3360 | 2587 | 0.39 | 339 | 0.89 | 0.95 | 0.58 | 0.02 | 4.05 | 94388 | 93809 |
| GMI | P | 0.5 | 39.36 | 19.45 | 3117 | 2366 | 0.00 | 191 | 0.84 | 0.89 | 2.94 | 0.31 | 10.50 | 94326 | 91399 |
| GMI | P | 0.75 | 39.35 | 19.36 | 3174 | 2421 | 0.02 | 263 | 0.87 | 0.92 | 1.30 | 0.10 | 7.38 | 94345 | 93052 |
| GMI | P | 1 | 39.31 | 19.26 | 3234 | 2476 | 0.07 | 342 | 0.86 | 0.91 | 0.21 | 0.01 | 4.61 | 94352 | 94148 |
| GMI+WS | - | 0.5 | 39.37 | 19.50 | 3043 | 2307 | 0.35 | 406 | 0.72 | 0.80 | 4.04 | 0.54 | 13.42 | 94285 | 90266 |
| GMI+WS | F | 0.75 | 39.37 | 19.48 | 3086 | 2346 | 0.38 | 435 | 0.80 | 0.87 | 3.00 | 0.33 | 10.88 | 94306 | 91321 |
| GMI+WS | F | 1 | 39.35 | 19.44 | 3114 | 2372 | 0.42 | 466 | 0.82 | 0.89 | 1.85 | 0.17 | 9.10 | 94322 | 92477 |
| GMI+WS | P | 0.5 | 39.35 | 19.46 | 2976 | 2246 | 0.05 | 405 | 0.74 | 0.76 | 3.44 | 0.44 | 12.71 | 94289 | 90871 |
| GMI+WS | P | 0.75 | 39.33 | 19.39 | 2969 | 2245 | 0.07 | 435 | 0.74 | 0.77 | 2.42 | 0.25 | 10.10 | 94290 | 91879 |
| GMI+WS | P | 1 | 39.31 | 19.37 | 3041 | 2306 | 0.10 | 466 | 0.78 | 0.80 | 1.12 | 0.11 | 9.59 | 94299 | 93182 |
| UBI | . | 0.5 | 39.35 | 19.48 | 3170 | 2426 | 0.38 | 568 | 0.86 | 0.92 | 1.28 | 0.10 | 7.43 | 94348 | 93079 |
| UBI | F | 0.75 | 39.31 | 19.35 | 3166 | 2430 | 0.47 | 814 | 0.84 | 0.89 | 0.12 | 0.01 | 6.13 | 94361 | 94238 |
| UBI | F | 1 | 39.23 | 19.07 | 3027 | 2317 | 0.58 | 1060 | 0.69 | 0.71 | 0.00 | 0.00 | 0.00 | 94328 | 94328 |
| UBI | P | 0.5 | 39.31 | 19.40 | 3064 | 2334 | 0.11 | 568 | 0.83 | 0.83 | 0.62 | 0.05 | 7.97 | 94340 | 93727 |
| UBI | P | 0.75 | 39.23 | 19.15 | 2951 | 2244 | 0.22 | 814 | 0.67 | 0.67 | 0.06 | 0.00 | 2.94 | 94313 | 94258 |
| UBI | P | 1 | 39.08 | 18.67 | 2646 | 1986 | 0.38 | 1060 | 0.38 | 0.44 | 0.00 | 0.00 | 0.00 | 94206 | 94206 |
| UBI+WS | F | 0.5 | 39.37 | 19.51 | 3069 | 2333 | 0.37 | 599 | 0.79 | 0.85 | 3.49 | 0.43 | 12.25 | 94300 | 90830 |
| UBI+WS | F | 0.75 | 39.36 | 19.48 | 3113 | 2374 | 0.41 | 721 | 0.83 | 0.89 | 2.21 | 0.21 | 9.65 | 94323 | 92128 |
| UBI+WS | F | 1 | 39.34 | 19.43 | 3131 | 2394 | 0.44 | 844 | 0.84 | 0.90 | 1.02 | 0.08 | 7.66 | 94337 | 93322 |
| UBI+WS | P | 0.5 | 39.35 | 19.43 | 2988 | 2264 | 0.09 | 598 | 0.78 | 0.79 | 2.58 | 0.27 | 10.46 | 94303 | 91732 |
| UBI+WS | P | 0.75 | 39.31 | 19.34 | 2960 | 2248 | 0.11 | 720 | 0.74 | 0.73 | 1.00 | 0.08 | 7.62 | 94301 | 93311 |
| UBI+WS | P | 1 | 39.26 | 19.24 | 2964 | 2249 | 0.16 | 841 | 0.66 | 0.64 | 0.27 | 0.01 | 3.56 | 94281 | 94013 |
| WS | F | 0.5 | 39.37 | 19.53 | 2944 | 2225 | 0.34 | 353 | 0.57 | 0.63 | 4.67 | 0.76 | 16.33 | 94258 | 89610 |
| WS | F | 0.75 | 39.36 | 19.53 | 2940 | 2224 | 0.36 | 352 | 0.62 | 0.66 | 4.17 | 0.62 | 14.88 | 94265 | 90120 |
| WS | F | 1 | 39.36 | 19.53 | 2933 | 2221 | 0.39 | 352 | 0.65 | 0.68 | 3.65 | 0.50 | 13.79 | 94271 | 90646 |
| WS | P | 0.5 | 39.35 | 19.50 | 2895 | 2180 | 0.04 | 352 | 0.63 | 0.62 | 4.18 | 0.64 | 15.19 | 94266 | 90106 |
| WS | P | 0.75 | 39.34 | 19.47 | 2857 | 2153 | 0.04 | 352 | 0.57 | 0.54 | 3.63 | 0.52 | 14.45 | 94258 | 90649 |
| WS | P | 1 | 39.34 | 19.52 | 2920 | 2206 | 0.07 | 351 | 0.67 | 0.65 | 3.01 | 0.38 | 12.46 | 94268 | 91273 |

Table C.4. Equilibrium: $\boldsymbol{\eta}=\mathbf{- 0 . 5}$

| (a) |  |  | (b) | (c) | (d) | (e) | (f) | (g) | (h) | (i) | (1) | (m) | (n) | (o) | (p) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  | 耧 |  | $\begin{aligned} & \text { 긍 } \\ & \text { O } \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |  |  | $\begin{aligned} & 3 \\ & 0 \end{aligned}$ | $\begin{aligned} & 3 \\ & \text { U } \\ & \text { E } \end{aligned}$ |
| CURRENT |  |  | 39.35 | 19.45 | 2930 | 2191 | -- | 101 | -- | -- | 4.23 | 0.58 | 13.71 | 94255 | 90047 |
| GMI | F | 0.5 | 39.31 | 19.27 | 2923 | 2202 | 0.31 | 193 | 0.46 | 0.60 | 3.09 | 0.32 | 10.37 | 94248 | 91176 |
| GMI | F | 0.75 | 39.26 | 19.10 | 2906 | 2191 | 0.38 | 269 | 0.42 | 0.58 | 0.92 | 0.06 | 0.61 | 94247 | 93333 |
| GMI | F | 1 | 39.21 | 18.94 | 2889 | 2183 | 0.45 | 356 | 0.41 | 0.54 | 0.00 | 0.00 | 0.18 | 94251 | 94248 |
| GMI | P | 0.5 | 39.30 | 19.29 | 2921 | 2198 | 0.02 | 193 | 0.59 | 0.65 | 2.50 | 0.26 | 10.47 | 94269 | 91785 |
| GMI | P | 0.75 | 39.26 | 19.12 | 2903 | 2189 | 0.05 | 269 | 0.52 | 0.59 | 0.65 | 0.05 | 7.41 | 94262 | 93613 |
| GMI | P | 1 | 39.19 | 18.93 | 2877 | 2169 | 0.14 | 356 | 0.43 | 0.52 | 0.01 | 0.00 | 0.23 | 94242 | 94237 |
| GMI+WS | F | 0.5 | 39.33 | 19.42 | 2932 | 2211 | 0.36 | 406 | 0.52 | 0.62 | 3.88 | 0.51 | 13.19 | 94256 | 90398 |
| GMI+WS | F | 0.75 | 39.31 | 19.34 | 2923 | 2206 | 0.40 | 435 | 0.54 | 0.64 | 2.77 | 0.28 | 10.24 | 94260 | 91511 |
| GMI+WS | F | 1 | 39.29 | 19.28 | 2916 | 2202 | 0.45 | 467 | 0.56 | 0.64 | 1.54 | 0.12 | 8.07 | 94266 | 92732 |
| GMI+WS | P | 0.5 | 38.76 | 20.13 | 2937 | 2212 | 0.06 | 408 | 0.63 | 0.70 | 3.43 | 0.42 | 12.29 | 94279 | 90864 |
| GMI+WS | P | 0.75 | 38.72 | 20.08 | 2929 | 2210 | 0.07 | 437 | 0.63 | 0.68 | 2.36 | 0.24 | 10.05 | 94278 | 91928 |
| GMI+WS | P | 1 | 38.66 | 20.00 | 2912 | 2193 | 0.13 | 468 | 0.54 | 0.57 | 0.81 | 0.09 | 11.17 | 94258 | 93455 |
| UBI | F | 0.5 | 39.27 | 19.26 | 2910 | 2202 | 0.41 | 568 | 0.56 | 0.62 | 0.87 | 0.06 | 7.08 | 94270 | 93410 |
| UBI | F | 0.75 | 39.22 | 19.09 | 2889 | 2190 | 0.51 | 814 | 0.52 | 0.57 | 0.06 | 0.00 | 3.11 | 94272 | 94215 |
| UBI | F | 1 | 39.16 | 18.93 | 2867 | 2178 | 0.60 | 1060 | 0.51 | 0.56 | 0.00 | 0.00 | 0.00 | 94273 | 94273 |
| UBI | P | 0.5 | 39.26 | 19.26 | 2902 | 2195 | 0.13 | 568 | 0.62 | 0.62 | 0.52 | 0.04 | 6.96 | 94289 | 93770 |
| UBI | P | 0.75 | 39.20 | 19.09 | 2877 | 2180 | 0.23 | 814 | 0.57 | 0.59 | 0.04 | 0.00 | 2.78 | 94287 | 94252 |
| UBI | P | 1 | 39.13 | 18.92 | 2850 | 2164 | 0.33 | 1060 | 0.53 | 0.58 | 0.00 | 0.00 | 0.00 | 94281 | 94281 |
| UBI+WS | F | 0.5 | 39.32 | 19.40 | 2928 | 2212 | 0.38 | 598 | 0.56 | 0.65 | 3.32 | 0.40 | 12.07 | 94262 | 90961 |
| UBI+WS | F | 0.75 | 39.30 | 19.33 | 2920 | 2208 | 0.42 | 720 | 0.57 | 0.65 | 1.96 | 0.18 | 8.90 | 94268 | 92316 |
| UBI+WS | F | 1 | 39.27 | 19.24 | 2910 | 2203 | 0.47 | 843 | 0.56 | 0.62 | 0.73 | 0.05 | 6.38 | 94272 | 93545 |
| UBI+WS | P | 0.5 | 39.31 | 19.42 | 2924 | 2208 | 0.09 | 598 | 0.68 | 0.69 | 2.52 | 0.26 | 10.14 | 94288 | 91778 |
| UBI+WS | P | 0.75 | 39.27 | 19.34 | 2911 | 2205 | 0.12 | 720 | 0.64 | 0.64 | 0.89 | 0.07 | 7.70 | 94290 | 93405 |
| UBI+WS | P | 1 | 39.21 | 19.21 | 2886 | 2180 | 0.18 | 841 | 0.51 | 0.53 | 0.23 | 0.01 | 2.61 | 94257 | 94029 |
| WS | F | 0.5 | 39.36 | 19.55 | 2940 | 2222 | 0.34 | 353 | 0.55 | 0.62 | 4.64 | 0.76 | 16.43 | 94262 | 89650 |
| WS | F | 0.75 | 39.35 | 19.55 | 2938 | 2223 | 0.36 | 352 | 0.59 | 0.66 | 4.16 | 0.62 | 14.95 | 94270 | 90137 |
| WS | F | 1 | 39.34 | 19.56 | 2936 | 2223 | 0.39 | 352 | 0.62 | 0.68 | 3.65 | 0.50 | 13.79 | 94277 | 90651 |
| WS | P | 0.5 | 39.35 | 19.57 | 2938 | 2218 | 0.03 | 352 | 0.66 | 0.71 | 4.18 | 0.65 | 15.57 | 94285 | 90131 |
| WS | P | 0.75 | 39.35 | 19.57 | 2937 | 2222 | 0.03 | 352 | 0.68 | 0.73 | 3.63 | 0.54 | 14.82 | 94289 | 90677 |
| WS | P | 1 | 39.33 | 19.55 | 2928 | 2213 | 0.06 | 352 | 0.64 | 0.66 | 3.01 | 0.38 | 12.59 | 94275 | 91280 |

Table C.5. Equilibrium: $\boldsymbol{\eta}=-\mathbf{1}$

| (a) |  |  | (b) | (c) | (d) | (e) | (f) | (g) | (h) | (i) | (1) | (m) | (n) | (o) | (p) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | $\begin{aligned} & \text { an } \\ & \text { on } \\ & 0.0 \\ & 0.0 \end{aligned}$ |  |  |  | 晋 |  |  |  |  | $3$ | $\begin{aligned} & 3 \\ & 0 \\ & 0 \\ & 2 \end{aligned}$ |
| CURRENT |  |  | 39.35 | 19.45 | 2930 | 2191 | -- | 101 | -- | -- | 4.23 | 0.58 | 13.71 | 94255 | 90047 |
| GMI | F | 0.5 | 39.30 | 19.29 | 2925 | 2204 | 0.31 | 193 | 0.54 | 0.60 | 3.09 | 0.32 | 10.40 | 94254 | 91181 |
| GMI | F | 0.75 | 39.25 | 19.13 | 2911 | 2197 | 0.37 | 269 | 0.53 | 0.60 | 0.93 | 0.06 | 6.82 | 94257 | 93332 |
| GMI | F | 1 | 39.20 | 18.95 | 2892 | 2187 | 0.45 | 356 | 0.47 | 0.54 | 0.01 | 0.00 | 0.24 | 94255 | 94250 |
| GMI | P | 0.5 | 39.29 | 19.31 | 2923 | 2200 | 0.01 | 193 | 0.64 | 0.66 | 2.50 | 0.26 | 10.49 | 94275 | 91790 |
| GMI | P | 0.75 | 39.25 | 19.13 | 2906 | 2192 | 0.05 | 269 | 0.58 | 0.60 | 0.84 | 0.05 | 5.89 | 94268 | 93431 |
| GMI | P | 1 | 39.18 | 18.94 | 2880 | 2173 | 0.14 | 356 | 0.48 | 0.52 | 0.01 | 0.00 | 0.38 | 94246 | 94241 |
| GMI+WS | F | 0.5 | 39.32 | 19.44 | 2933 | 2213 | 0.36 | 406 | 0.58 | 0.62 | 3.90 | 0.51 | 13.18 | 94263 | 90383 |
| GMI+WS | F | 0.75 | 39.30 | 19.37 | 2927 | 2210 | 0.40 | 435 | 0.62 | 0.65 | 2.79 | 0.29 | 10.23 | 94269 | 91495 |
| GMI+WS | F | 1 | 39.28 | 19.29 | 2918 | 2204 | 0.45 | 467 | 0.61 | 0.64 | 1.55 | 0.13 | 8.17 | 94272 | 92735 |
| GMI+WS | P | 0.5 | 39.32 | 19.45 | 2930 | 2208 | 0.06 | 405 | 0.68 | 0.70 | 3.44 | 0.42 | 12.33 | 94284 | 90865 |
| GMI+WS | P | 0.75 | 39.29 | 19.38 | 2923 | 2206 | 0.07 | 435 | 0.67 | 0.69 | 2.31 | 0.24 | 10.29 | 94284 | 91987 |
| GMI+WS | P | 1 | 39.25 | 19.29 | 2908 | 2192 | 0.12 | 466 | 0.60 | 0.58 | 0.81 | 0.09 | 11.24 | 94266 | 93460 |
| UBI | F | 0.5 | 39.26 | 19.28 | 2913 | 2205 | 0.41 | 568 | 0.61 | 0.63 | 0.88 | 0.06 | 7.08 | 94276 | 93404 |
| UBI | F | 0.75 | 39.21 | 19.12 | 2895 | 2196 | 0.50 | 814 | 0.58 | 0.57 | 0.06 | 0.00 | 3.37 | 94282 | 94225 |
| UBI | F | 1 | 39.15 | 18.95 | 2872 | 2184 | 0.60 | 1060 | 0.54 | 0.56 | 0.00 | 0.00 | 0.00 | 94281 | 94281 |
| UBI | P | 0.5 | 39.25 | 19.29 | 2907 | 2199 | 0.13 | 568 | 0.66 | 0.62 | 0.52 | 0.04 | 7.10 | 94298 | 93779 |
| UBI | P | 0.75 | 39.19 | 19.12 | 2883 | 2186 | 0.23 | 814 | 0.61 | 0.59 | 0.04 | 0.00 | 3.01 | 94297 | 94261 |
| UBI | P | 1 | 39.12 | 18.94 | 2856 | 2170 | 0.33 | 1060 | 0.57 | 0.58 | 0.00 | 0.00 | 0.00 | 94290 | 94290 |
| UBI+WS | F | 0.5 | 39.31 | 19.42 | 2929 | 2213 | 0.38 | 598 | 0.60 | 0.65 | 3.32 | 0.40 | 12.10 | 94267 | 90966 |
| UBI+WS | F | 0.75 | 39.29 | 19.34 | 2922 | 2210 | 0.42 | 720 | 0.63 | 0.66 | 1.97 | 0.18 | 8.97 | 94274 | 92320 |
| UBI+WS | F | 1 | 39.26 | 19.26 | 2912 | 2206 | 0.47 | 843 | 0.62 | 0.62 | 0.73 | 0.05 | 6.48 | 94277 | 93550 |
| UBI+WS | P | 0.5 | 39.30 | 19.44 | 2925 | 2209 | 0.09 | 598 | 0.70 | 0.70 | 2.53 | 0.26 | 10.17 | 94295 | 91781 |
| UBI+WS | P | 0.75 | 39.26 | 19.37 | 2914 | 2208 | 0.11 | 720 | 0.69 | 0.65 | 0.90 | 0.07 | 7.69 | 94299 | 93408 |
| UBI+WS | P | 1 | 39.20 | 19.24 | 2891 | 2185 | 0.18 | 841 | 0.57 | 0.54 | 0.23 | 0.01 | 2.81 | 94266 | 94039 |
| WS | F | 0.5 | 39.35 | 19.57 | 2940 | 2223 | 0.34 | 353 | 0.62 | 0.62 | 4.64 | 0.76 | 16.41 | 94268 | 89651 |
| WS | F | 0.75 | 39.34 | 19.57 | 2938 | 2223 | 0.36 | 352 | 0.63 | 0.66 | 4.16 | 0.62 | 14.96 | 94274 | 90141 |
| WS | F | 1 | 39.33 | 19.58 | 2936 | 2224 | 0.39 | 352 | 0.66 | 0.69 | 3.65 | 0.50 | 13.78 | 94283 | 90652 |
| WS | P | 0.5 | 39.34 | 19.59 | 2938 | 2218 | 0.03 | 352 | 0.70 | 0.71 | 4.19 | 0.65 | 15.51 | 94290 | 90125 |
| WS | P | 0.75 | 39.34 | 19.59 | 2937 | 2223 | 0.03 | 352 | 0.72 | 0.73 | 3.63 | 0.54 | 14.87 | 94295 | 90683 |
| WS | P | 1 | 39.31 | 19.58 | 2930 | 2215 | 0.06 | 352 | 0.68 | 0.67 | 3.02 | 0.38 | 12.56 | 94283 | 91283 |

Table C.6. Equilibrium: $\boldsymbol{\eta}=-\infty$

| (a) |  |  | (b) | (c) | (d) | (e) | (f) | (g) | (h) | (i) | (1) | (m) | (n) | (o) | (p) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | $\begin{aligned} & \stackrel{0}{0} \\ & 0.0 \\ & . \ddot{~} \\ & \ddot{0} \end{aligned}$ |  |  | 晋覀 |  |  |  |  | $3$ | $\begin{aligned} & 3 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ |
| Current |  |  | 39.35 | 19.45 | 2930 | 2191 | -- | 101 | -- | -- | 4.23 | 0.58 | 13.71 | 94255 | 90047 |
| GMI | F | 0.5 | 39.28 | 18.62 | 2899 | 2167 | 0.32 | 198 | 0.06 | 0.49 | 2.88 | 0.30 | 10.56 | 94031 | 91173 |
| GMI | F | 0.75 | 39.19 | 17.83 | 2859 | 2135 | 0.39 | 281 | 0.04 | 0.42 | 0.76 | 0.05 | 6.03 | 93825 | 93077 |
| GMI | F | 1 | 39.10 | 17.06 | 2816 | 2104 | 0.48 | 379 | 0.05 | 0.42 | 0.00 | 0.00 | 0.00 | 93628 | 93628 |
| GMI | P | 0.5 | 39.27 | 18.65 | 2881 | 2163 | 0.02 | 197 | 0.07 | 0.54 | 2.39 | 0.25 | 10.34 | 94057 | 91683 |
| GMI | P | 0.75 | 39.19 | 17.89 | 2841 | 2134 | 0.07 | 280 | 0.06 | 0.46 | 0.59 | 0.04 | 6.63 | 93852 | 93267 |
| GMI | P | 1 | 39.08 | 17.08 | 2789 | 2091 | 0.17 | 378 | 0.06 | 0.42 | 0.00 | 0.00 | 0.00 | 93629 | 93629 |
| GMI+WS | F | 0.5 | 39.31 | 18.82 | 2909 | 2178 | 0.37 | 405 | 0.07 | 0.53 | 3.88 | 0.51 | 13.03 | 94058 | 90213 |
| GMI+WS | F | 0.75 | 39.25 | 18.20 | 2879 | 2153 | 0.41 | 436 | 0.05 | 0.47 | 2.55 | 0.26 | 10.35 | 93884 | 91358 |
| GMI+WS | F | 1 | 39.19 | 17.49 | 2844 | 2125 | 0.46 | 471 | 0.04 | 0.41 | 1.25 | 0.11 | 8.57 | 93684 | 92449 |
| GMI+WS | P | 0.5 | 39.30 | 18.84 | 2891 | 2173 | 0.06 | 405 | 0.08 | 0.61 | 3.35 | 0.42 | 12.44 | 94080 | 90752 |
| GMI+WS | P | 0.75 | 39.25 | 18.19 | 2859 | 2150 | 0.08 | 435 | 0.07 | 0.52 | 2.13 | 0.22 | 10.45 | 93890 | 91785 |
| GMI+WS | P | 1 | 39.16 | 17.47 | 2817 | 2111 | 0.14 | 470 | 0.05 | 0.42 | 0.76 | 0.08 | 10.33 | 93671 | 92918 |
| UBI | F | 0.5 | 39.25 | 18.67 | 2891 | 2171 | 0.41 | 568 | 0.09 | 0.54 | 0.86 | 0.06 | 6.83 | 94071 | 93220 |
| UBI | F | 0.75 | 39.16 | 17.92 | 2847 | 2139 | 0.52 | 814 | 0.08 | 0.49 | 0.04 | 0.00 | 3.59 | 93875 | 93840 |
| UBI | F | 1 | 39.06 | 17.14 | 2800 | 2103 | 0.62 | 1060 | 0.08 | 0.49 | 0.00 | 0.00 | 0.00 | 93669 | 93669 |
| UBI | P | 0.5 | 39.23 | 18.61 | 2865 | 2162 | 0.14 | 568 | 0.11 | 0.56 | 0.46 | 0.03 | 7.25 | 94070 | 93615 |
| UBI | P | 0.75 | 39.13 | 17.86 | 2818 | 2127 | 0.24 | 814 | 0.10 | 0.53 | 0.02 | 0.00 | 2.35 | 93870 | 93850 |
| UBI | P | 1 | 39.02 | 17.07 | 2765 | 2087 | 0.35 | 1060 | 0.09 | 0.51 | 0.00 | 0.00 | 0.00 | 93659 | 93659 |
| UBI+WS | F | 0.5 | 39.30 | 18.78 | 2905 | 2178 | 0.38 | 595 | 0.08 | 0.55 | 3.29 | 0.39 | 11.76 | 94057 | 90789 |
| UBI+WS | F | 0.75 | 39.24 | 18.10 | 2872 | 2152 | 0.43 | 715 | 0.07 | 0.47 | 1.95 | 0.17 | 8.48 | 93866 | 91932 |
| UBI+WS | F | 1 | 39.17 | 17.40 | 2836 | 2125 | 0.48 | 835 | 0.06 | 0.42 | 0.70 | 0.04 | 5.76 | 93669 | 92982 |
| UBI+WS | P | 0.5 | 39.29 | 18.85 | 2886 | 2175 | 0.10 | 595 | 0.10 | 0.61 | 2.58 | 0.26 | 10.01 | 94096 | 91537 |
| UBI+WS | P | 0.75 | 39.22 | 18.19 | 2850 | 2151 | 0.12 | 715 | 0.10 | 0.54 | 0.87 | 0.07 | 7.54 | 93904 | 93046 |
| UBI+WS | P | 1 | 39.12 | 17.46 | 2803 | 2107 | 0.19 | 833 | 0.07 | 0.44 | 0.09 | 0.00 | 4.17 | 93676 | 93589 |
| WS | F | 0.5 | 39.33 | 18.96 | 2900 | 2187 | 0.34 | 350 | 0.06 | 0.54 | 4.74 | 0.77 | 16.28 | 94066 | 89366 |
| WS | F | 0.75 | 39.29 | 18.40 | 2874 | 2167 | 0.37 | 348 | 0.06 | 0.51 | 4.08 | 0.62 | 15.15 | 93889 | 89854 |
| WS | F | 1 | 39.26 | 17.84 | 2848 | 2147 | 0.40 | 345 | 0.05 | 0.46 | 3.71 | 0.50 | 13.57 | 93720 | 90052 |
| WS | P | 0.5 | 39.33 | 18.91 | 2896 | 2181 | 0.04 | 350 | 0.07 | 0.62 | 4.21 | 0.64 | 15.23 | 94068 | 89888 |
| WS | P | 0.75 | 39.29 | 18.31 | 2868 | 2162 | 0.04 | 347 | 0.06 | 0.56 | 3.76 | 0.54 | 14.37 | 93875 | 90148 |
| WS | P | 1 | 39.23 | 17.73 | 2836 | 2133 | 0.07 | 344 | 0.05 | 0.43 | 2.96 | 0.38 | 12.83 | 93684 | 90755 |

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[^1]:    ${ }^{1}$ While we are writing, in the EU countries only Greece, Hungary and Italy do not implement a nation-wide minimum income policy. Since 1992 the European Commission has issued many declarations and recommendations where minimum income policies emerge as a key instrument for enforcing fundamental human rights, reducing poverty and promoting social inclusion. A useful survey of minimum income policies in Europe is provided by Busilacchi (2008). A detailed institutional analysis for Italy is found in Sacchi (2005).

[^2]:    ${ }^{2}$ Among the Western countries, Alaska's social dividend represents at the moment the only example of a pure (although of small amount) citizen's income. Unconditional transfer, however, are receiving an increasing attention in developing countries. Brazil in 2004 passed a law for the gradual introduction of a basic income and pilot experiences have been launched in South America, Africa and India.
    ${ }^{3}$ More from a macroeconomic perspective Meade (1995) argued in favour of a "citizen income" as a necessary mechanisms in a fullemployment capitalist society. Bowles (2002) and Groot and Peters (1997) develop theoretical general equilibrium models that support the feasibility and macroeconomic desirability of a universal basic income policy.

[^3]:    ${ }^{4}$ The "square root scale" is one of the equivalence scales commonly used in OECD publications.

[^4]:    ${ }^{5}$ A somewhat mitigated version has been proposed by Atkinson $(1995,1996)$ as Participation Income, where the transfer is conditional upon a test of "participation" (work, education, voluntary social activities, child care, homework etc.).
    ${ }^{6}$ A mixed system close to GMI+WS has been proposed by De Vincenti and Paladini (2009).

[^5]:    ${ }^{7}$ The choice probability is a simplified version of the one derived in Aaberge et al. (1999) and Aaberge and Colombino (2011), where however wage rates and other observed job characteristics can vary across jobs for the same households. A general formulation is given by Dagsvik (1994). The model is also close to Ben-Akiva and Watanatada (1981).

[^6]:    ${ }^{8}$ For a theoretical justification of this social welfare function (as a member of a wider class) see for example Aaberge (2007) and Aaberge and Colombino (2011).
    ${ }^{9}$ Current (1998) marginal tax rates are reported in Appendix B.

[^7]:    ${ }^{10}$ In favour of unconditional transfers there might be additional arguments such as those mentioned in Section 1.
    ${ }^{11}$ A recent survey by Diamond and Saez (2011) gives support to the superiority of progressive taxes. This conclusion might be mitigated or even reversed if one accounted for the transparency and simplicity of the tax rule, for incentives to tax elusion/evasion and in general for a more general concept of behavioural response to taxes as in the "taxable income" approach (e.g. Gruber and Saez 2002).

[^8]:    ${ }^{12}$ It should be noticed that the 101 Euros transfer in the CURRENT system is just the average of various categorical, conditional or local transfers and benefits (such as unemployment benefits, "cassa integrazione", family benefits etc.).

[^9]:    ${ }^{13}$ Surveys of various approaches to modelling labour supply for tax reform simulation are provided by Creedy et al. (2005), Bourguignon et al. (2006) and Meghir et al. (2008).

[^10]:    ${ }^{14}$ Expressions (A.3) and (A.7) are close to other multinomial logit models "augmented" by alternative-specific dummies (e.g. Van Soest, 1995; Kornstad and Thoresen, 2007). Here however we adopt a specific structural interpretation of the dummies' coefficients (A.8).
    ${ }^{15}$ A comparison and evaluation of different procedures to specify the choice set is provided by Aaberge et al. (2009).
    ${ }^{16}$ EUROMOD is a tax-benefit microsimulation model for the European Union that enables researchers and policy analysts to calculate, in a comparable manner, the effects of taxes and benefits on household incomes and work incentives for the population of each country and for the EU as a whole. EUROMOD was originally designed by a research team under the direction of Holly Sutherland at the Department of Economics in Cambridge ,UK. It is now developed and updated at the Microsimulation Unit at ISER (University of Essex, UK).

[^11]:    ${ }^{17}$ A different procedure for equilibrium simulation - which however would not be appropriate with our microeconometric model - has been proposed by Creedy and Duncan (2001).

[^12]:    ${ }^{18}$ For the derivation of this expression, see McFadden (1978) and Ben-Akiva et al. (1985). The same methodology for empirical welfare evaluation is used by Colombino (1998).
    ${ }^{19}$ A comprehensive explanation of the procedure adopted for developing interpersonally comparable measures of utility is provided by King (1983).

